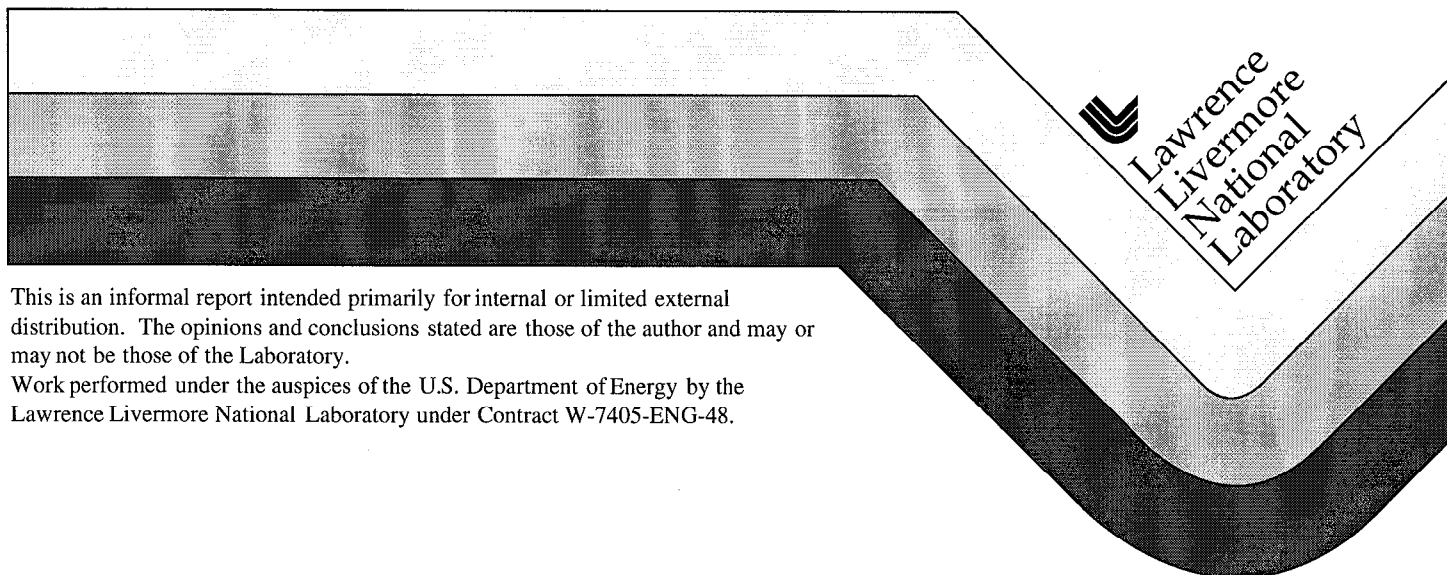


**Lung Cancer Risk of Low-Level Exposures to Alpha Emitters:
Critical Reappraisal and Experiments Based on a New Cytodynamic Model**

K. T. Bogen

February 20, 1999



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Lung Cancer Risk of Low-Level Exposures to Alpha Emitters: Critical Reappraisal and Experiments Based on a New Cytodynamic Model

Final Report on LDRD Project 97-ERD-050

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February 20, 1999

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Summary

Ecologic U.S. county data suggest negative associations between residential radon exposure and lung cancer mortality (LCM)—inconsistent with clearly positive associations revealed by occupational data on individual miners, but perhaps explained by competing effects of cell killing vs. mutations in alpha-exposed bronchial epithelium. To assess the latter possibility, a biologically based “cytodynamic 2-stage” (CD2) cancer-risk model was fit to combined 1950-54 age-specific person-year data on lung cancer mortality (LCM) in white females of age 40+ y in 2,821 U.S. counties (~90% never-smokers), and in 5 cohorts of underground miners who never smoked. New estimates of household annual average radon exposure in U.S. counties were used, which were found to have a significant negative ecologic association with 1950-54 LCM in U.S. white females, adjusted for age and all subsets of two among 21 socioeconomic, climatic and other factors considered. A good CD2 fit was obtained to the combined residential/miner data, using biologically plausible parameter values. Without further optimization, the fit also predicted independent inverse dose-rate effects shown (for the first time) to occur in nonsmoking miners. Using the same U.S. county-level LCM data, a separate study revealed a positive ecologic association between LCM and bituminous coal use in the U.S., in agreement with epidemiological data on LCM in women in China. The modeling results obtained are consistent with the CD2-based hypothesis that residential radon exposure has a nonlinear U-shaped relation to LCM risk, and that current linear no-threshold extrapolation models substantially overestimate such risk. A U-shaped dose-response corresponds to a CD2-model prediction that alpha radiation kills more premalignant cells than it generates at low exposure levels, but not at higher levels. To test this hypothesis, groups of Japanese medaka (ricefish minnows) were exposed for 10 to 14 weeks to different concentrations of aqueous radon; histological and quantitative-morphometry analysis of proliferative (premalignant) foci in livers from these fish are currently being completed.

Acknowledgments

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1. Introduction and Overview

This report describes the focus, methods and results of three related research efforts undertaken during FY97-FY98 comprising LLNL LDRD Project 97-ERD-050. These three research efforts concerned: (1) application of a mechanistic, biologically based cancer-risk model to apparently contradictory epidemiological data relating lung-cancer mortality (LCM) to residential and occupational exposures to radon gas; (2) a parallel assessment of whether the same U.S. county-level LCM data used for the latter analysis revealed an expected positive association between LCM and lifetime use of bituminous coal for residential heating; and (3) an experimental test of a biologically based hypothesis that premalignant-cell number (and by implication, cancer risk) may have a nonlinear dose-response relation to alpha radiation. An introduction and overview of these three efforts is provided below, followed by detailed descriptions in Sections 2, 3 and 4 of this report.

The present LDRD research project stemmed from the observation that a new, cytodynamic two-stage (CD2) cancer model developed at LLNL was able to predict two apparently contrasting data sets relating lung-cancer mortality (LCM) to radon exposure (Bogen, 1997). First, the model predicted a negative dose-response trend when previously published U.S. county-level data on mean residential radon exposures were compared to data on age-adjusted 1980s LCM in white males (both smokers and nonsmokers); second, the model predicted a positive dose-response trend when summary information on cumulative occupational radon exposure was compared to previously published summary LCM estimates for underground miners working on the Colorado Plateau. That both data sets were fit using one set

of biologically realistic CD2-parameter values suggested that low-level radon may actually reduce lung cancer risk, that is, that the negative ecologic association between radon and LCM risk may be biologically plausible, in view of the mechanistically realistic two-stage carcinogenesis theory on which the CD2 model is based. The CD2 model's prediction is based on the expectation of competing effects on cancer risk due to critical DNA damage vs. cell killing caused by the alpha irradiation of bronchial surface epithelium associated with the radioactive decay of naturally occurring radon gas. Specifically, in the case of radiation due to exposures to the small concentrations of radon gas typically found in U.S. homes, this radiation may kill enough premalignant cells to more than offset radiation-induced occurrence of new premalignant cells. Higher levels of radiation, however, are expected to increase lung-cancer risk by inducing the replacement of killed surface cells via proliferation of underlying stem cells, which in turn promotes the clonal expansion of any pre-existing "spontaneous" premalignant cells within the underlying (and relatively unexposed) stem cells.

Although biologically plausible, the preliminary CD2 modeling results (Bogen, 1997) relied entirely on a previously published summary of age-adjusted LCM and radon-exposure data, as well as on summary (rather than individual-level) data on LCM in Colorado Plateau uranium miners. The preliminary study also estimated the amount of cell killing caused by alpha radiation by means of fitting the CD2-model to LCM data, rather than using published estimates from *in vitro* experiments involving alpha-exposed human lung cells.

The primary goal of the present research project, therefore, was to refit the CD2 model for radon to sets of epidemiological data different than those used initially by Bogen (1987)—data that better address the estimation of radon concentrations in U.S. homes, as well as potentially confounding effects of smoking on the interpretation of radon-LCM associations. Specially, the limitations mentioned above were addressed by refitting the CD2 model, conditional on likely alpha cytotoxicity, to age-specific LCM data for white females of age 40+ y in 2,821 U.S. counties during 1950-54 (~90% of whom never smoked). Entirely new estimates of county-specific mean residential radon levels were used, together with age-specific (not age-adjusted) LCM data obtained for five cohorts of underground miners who never smoked.

During FY97, we assembled new data on age-specific LCM data and estimated corresponding residential radon concentrations in white females of age 40+ y (about 11% of whom ever smoked) in 2,821 U.S. counties during 1950–54, and in five different groups of underground miners (a total of 2,488 miners worldwide) who never smoked. The county-level LCM data for white women in the early 1950s, previously unavailable in any form, were generated from raw U.S. mortality data specifically for this study. We used new estimates of county-specific mean residential radon levels for all U.S. counties recently generated by Lawrence Berkeley National Laboratory (LBNL). In collaboration with LLNL, LBNL performed uncertainty analyses pertaining to the new radon estimates used. A data base of corresponding county-level census, climatological, and geophysical data were also assembled at LLNL. Person–year data summarizing individual-level exposure

and LCM information on nonsmoking miners were obtained through the National Cancer Institute.

Research during FY98 began with a trend-analysis of the improved “ecologic”-type epidemiological data, followed by a refit of the CD2 model to these data (Bogen, 1998). The trend analysis revealed that radon levels were found to be significantly negatively associated with corresponding county-level LCM rates in U.S. women who died in 1950–54 at age 40+ or 60+ years, after adjustment for age and subsets of 21 other factors considered. A similarity in results obtained for 40+ and 60+ year-olds indicates that inter-county differences in smoking are unlikely to explain the observed negative associations. A good CD2 fit was obtained to the combined residential and occupational data involving >50 data points relating radon exposure to age-specific LCM. This fit also happens also to predict the so-called “inverse dose-rate” effect observed previously in underground miners—but now shown—for the first time—also to occur in nonsmoking miners in particular (Bogen, 1998). Specifically, the CD2 fit obtained in this study predicts independent data to which the CD2 model was not fit—a result similar to that found previously using data on combined smoking and nonsmoking miners (Bogen, 1997). The results of this study are consistent with the hypothesis that residential radon exposure has a nonlinear, U-shaped relation to LCM risk, and that current linear extrapolation models may substantially overestimate such risk (Bogen, 1998).

A parallel analysis was also conducted to determine whether, using the same county-level data on LCM in white U.S. women during 1950-54 and corresponding geophysical/socioeconomic/climatic covariates generated for this study, an expected

positive ecologic association could be discerned between LCM and domestic exposure to bituminous coal (BC). Ecologic and case-control epidemiological studies on populations of women in China have shown a strong link between domestic BC exposure and lung cancer, but this association had never been studied in any U.S. population. For this purpose, historical county-level data on U.S. domestic BT use were obtained, and these data were compared to our corresponding LCM data for all counties in which 50% or more of homes used coal for heating. We found that BC use was—as expected—significantly positively associated with corresponding county-level LCM rates in U.S. women dying in 1950–54 at age 40+ or 60+ years, after adjustment for age and many other factors considered (Cullen and Bogen, 1998).

Experimental work was also conducted as part of this LDRD-sponsored project, in collaboration with Drs. M. Okihiro and D. Hinton of the University of California, Davis (U.C. Davis), School of Veterinary Medicine. The experimental work involved subchronic exposure of three groups of 148 Japanese medaka fish (rice-fish minnows) to different aqueous concentrations of radon gas at LLNL. The purpose of the study was to examine effects of alpha exposure (arising from the decay of radon, which partitions into fish livers at a concentration proportional to that of radon in tank water) on the occurrence and growth of premalignant cells (namely, enzymatically altered proliferative “foci”) in the livers of young fish exposed subchronically to different concentrations of radon gas. A separate experiment measured the tissue:water partition coefficient for radon between medaka soft tissue and surrounding tank water. Examination of fish livers from the primary study are currently being completed at U.C. Davis.

Detailed descriptions of the three efforts summarized above are provided in Sections 2, 3 and 4 of this report, respectively, which follow. Each section is divided into background, methods, results and (where applicable) discussion subsections. Overall conclusions of this project are discussed in Section 5.

2. Investigation of a Mechanistic Model Relating Radon Exposure to Lung-Cancer Risk Reflected in Combined Occupational and U.S. Residential Data

2.1 Background

Lung cancer mortality (LCM) risk from residential radon exposure is generally estimated by linear-no-threshold extrapolation from data on LCM in miners, and currently is thought to pose the greatest indoor air-pollution threat in the U.S., causing ~10% of all lung cancer and ~20-30% of all lung cancer in nonsmokers (NRC, 1988,1998; Puskin, 1992). In contrast, ecologic data on county-level U.S. residential radon exposures appear negatively associated with corresponding *age-adjusted* LCM rates in male or female U.S. smokers+nonsmokers during the 1980s, inconsistent with linear-no-threshold predictions (Cohen, 1995,1997). The observed negative association, however, is based on analyses of ecologic (in this case, county-level rather than individual-level) data, which are subject to unavoidable potential biases (Morgenstern, 1982; Piantadosi, 1994; Piantadosi *et al.*, 1988), such as within-county confounding due to smoking and age (Lubin, 1998; Smith *et al.*, 1998).

In view of controversy regarding lung cancer risks posed by residential radon exposure, it is interesting that Cohen's negative association at residential exposure

levels, and elevated LCM in miners, were jointly predicted by a mechanistic “cytodynamic 2-stage” (CD2) model of lung cancer using biologically plausible parameter estimates (Bogen, 1997). The CD2 fit obtained also happened to predict “inverse dose-rate” effects seen in miners, i.e., the greater risks observed in miners exposed over longer durations conditional on any given level of cumulative exposure (see (Lubin *et al.*, 1994,1995a). The CD2 model realistically assumes linear-no-threshold dose-response relations for alpha-induced cell killing and critical mutations (Bogen, 1997). Previous 2-stage stochastic “MVK”-model applications to radon presumed that premalignant-cell growth increases monotonically with cytotoxic radon dose (Luebeck *et al.*, 1996; Moolgavkar *et al.*, 1993). In contrast, the CD2 model may reflect net cytotoxic loss induced in exposed *premalignant* as well as exposed normal cells, and thus predict *reduced* cancer risk whenever: (i) induced cytotoxicity is sufficient to negate a slight net proliferative advantage presumed for spontaneous premalignant clones, but (ii) induced mutations yield too few new premalignant clones to offset the latter effect on tumor likelihood.

Although biologically plausible, the previous CD2 modeling results (Bogen, 1997) relied entirely on Cohen’s ecologic LCM and radon-exposure data, as well as on summary (rather than individual-level) data on LCM in Colorado Plateau uranium miners in specified ranges of cumulative occupational radon exposure (NRC, 1988). The previous CD2 study was also limited by its focus on lifetime rather than age-specific LCM risk (since different patterns of age-specific risk over time can yield the same pattern of lifetime risk as a function of dose), and by the fact that a parameter governing alpha cytotoxic potency was estimated rather than fixed at a likely value.

In the present study, each of these limitations was addressed by refitting the CD2 model, conditional on likely alpha cytotoxicity, to age-specific LCM data for white females of age 40+ y in 2,821 U.S. counties during 1950-54 (~90% of whom never smoked). Entirely new estimates of county-specific mean residential radon levels were used, together with age-specific LCM data obtained for five cohorts of underground miners who never smoked. The "inverse dose-rate" effect predicted by the new CD2 fit was also compared to LCM vs. dose-rate data pertaining to these miners. The partly ecologic design of this study (discussed below) did not remove any of the fundamental limitations posed by ecologic data use (noted above). Rather, this study was intended to better address the biological plausibility of apparent nonlinearity in dose-response for radon-induced lung cancer.

2.2. Materials and Methods

Residential Mortality and Smoking Data. Age- and county-specific 1950-54 LCM rates were obtained for U.S. white females (WF) aged 0-4, 5-9, ..., 85+ y, excluding data for Virginia considered unreliable at the county level for that period (Marsh *et al.*, 1996). Analyses excluded data on women <40 y for whom LCM was quite rare. Only ~11% (vs. ~5%) of WF who died at 40+ (vs. 60+) y in 1950-54 ever smoked, based on survey data covering this period (Haenszel and Shimkin, 1956; Mills and Porter, 1953). WF data were modeled for age <80 y only because the general pattern of LCM increase (a nearly cubic function of age) did not hold for older women. Such an apparent mortality-rate decline among the oldest age groups, which pertains to many types of cancer (Armitage and Doll, 1957), may be due to data unreliability (Doll and Peto, 1981) and/or population heterogeneity in cancer susceptibility,

neither of which are addressed by the CD2 model.

Rn-Exposure, Socioeconomic and Climatic Data for U.S. Counties. In addition to VA data noted above, data for major retirement states (AZ, CA, FL) were dropped in view of survey data indicating a large fraction of lifetime spent near residence at time of death in non-retirement states (Cohen, 1992b), expected even more so for WF dying in 1950-54. New estimates of annual-average household radon concentrations for the remaining 2,821 U.S. counties were used, based on ~4,700 annual-average (long-term) and ~50,000 3-day (short-term) radon U.S. Environmental Protection Agency national random-survey data. To obtain the new estimates, the latter survey data were systematically adjusted and interpolated to non-sampled counties using Monte-Carlo and regression methods, which incorporated county-level data on climatic and geophysical variates known to correlate with residential radon levels (Price, 1997; Price *et al.*, 1998). The geometric mean levels were scaled uniformly to corresponding arithmetic means, assuming lognormal intra-county distributions with a common approximate geometric standard deviation of 2 (Cohen, 1992a; Price, 1999; Price, 1997).

Among the resulting new county-level estimates of household radon, 1,683 pertain to counties for which corresponding estimates were made previously using *ad hoc* methods to combine survey data obtained from multiple sources (Cohen, 1995). The latter and former estimates are fairly well correlated: $R^2 = 0.733$. For residential exposures, 1 pCi/liter (=0.037 Bq) of radon in air was assumed to correspond to an annual exposure to 0.1935 “working level months” (WLM) of effective alpha energy (Puskin, 1992).

Additionally, 12 types of 1950 demographic/socioeconomic data (USBC, 1953), 5 typical 1953-1975 climatic measures (Apte *et al.*, 1997), weighted mean county elevation using census-tract populations as weights, and county-centroid latitude were each binned into county quintiles and were, together with a 3-level dietary Se index (Clark *et al.*, 1991) and U.S. region (among 9), included in pairs as factors used in addition to age (within 10-y bins) in preliminary analyses of adjusted trend. Significant and generally similar negative (ecologic) trends for LCM vs. radon were obtained for all 210 sets of the 22 adjustment factors used (see Results). Therefore, for modeling purposes, county-level age-specific LCM data were adjusted by one representative factor (family-income quintile) and then pooled within 6 ranges of estimated annual average household radon exposure (corresponding to median radon concentrations of <0.394, 0.394-0.787, 0.787-1.38, 1.38-2.17, 2.17-3.15, and >3.15 pCi/L).

Occupational Data. Information from 5 of 6 cohorts for which data on LCM in nonsmoking underground miners are available (Lubin *et al.*, 1994,1995a; NRC, 1998) was kindly provided by Dr. J. Lubin and coworkers. These person-year (PY) data ($n = 2,488$, 44,600.7 PY, 53 cases) were summarized by total LCM, PY and corresponding PY-weighted median values of attained age in y (AGE), age at first exposure in y (AGE_0), calendar year of follow-up (YR), exposure duration in y excluding the 5 y prior to attained age (DUR), and cumulative exposure in WLM up to 5 y prior to attained age (WLM), for the five WLM bins and three attained-age bins used by Lubin *et al.*, (1994, pp. 84-5), and for DUR ranges of 0-7, 8-15, and ≥ 16 y.

Cancer Risk Model. The CD2 model (Figure 1) was used with the changes

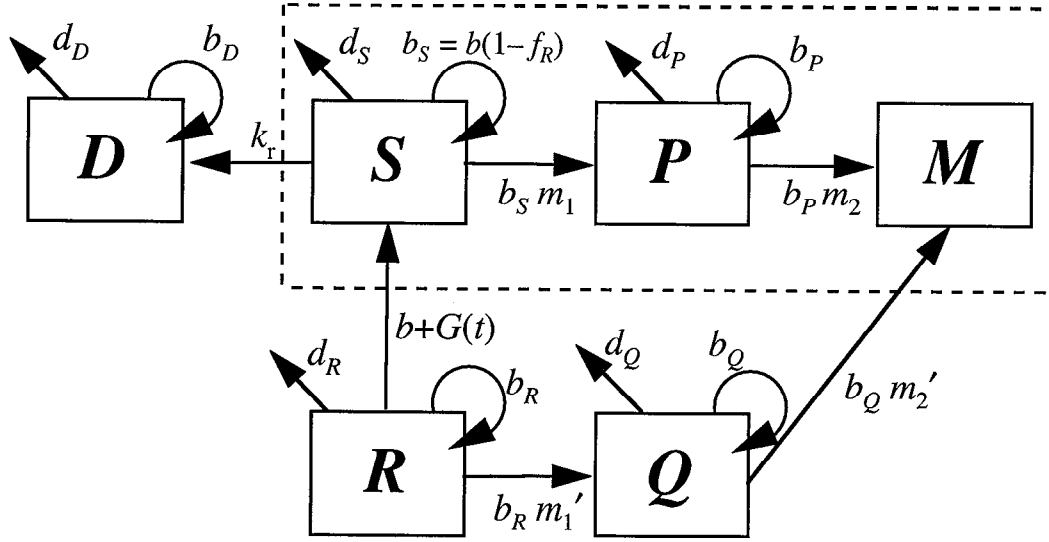


Figure 1. Cytodynamic 2-stage (CD2) model of bronchial carcinogenesis (Bogen, 1997), incorporating the “MVK” stochastic 2-stage framework (dashed box; see Moolgavkar, 1983) whereby normal epithelial stem cells (S) may each with probability m_1 per cell division give rise to a pre-malignant cell (P), which may proliferate clonally and with probability m_2 give rise to a malignant cell (M). The CD2 model adds a reservoir of unexposed cells (R) that may play a alpha-enhanced role in replacing S -cells lost at rate k_r to become reproductively dead cells (D). R -cells may progress to pre-malignant (Q) and malignant (M) cells via a process parallel to yet independent from the $S \rightarrow P \rightarrow M$ process. Rates of birth (b) and death/differentiation (d) are specified for each cell type, f_R is the ratio R/S under normal conditions.

noted. This model adapts the “MVK” 2-stage mechanistic framework, in which transition of normal (S) to premalignant (P) cells and of P -cells to malignant cells (M) is modeled as a doubly stochastic filtered Poisson process (Moolgavkar, 1983; Moolgavkar *et al.*, 1993). As applied to radon, the CD2 model additionally assumes: (i) alpha-induced transition from S to a pool of reproductively dead cells (D), (ii) replacement of S -cells partly by virtually unexposed cells (R) via a Verhulst feedback-inhibition process (where f_R denotes the ratio R/S under noncytotoxic conditions), and (iii) similarly unexposed premalignant (Q) cells derived from R -cells and subject to malignant transformation via a process similar to and independent from the $S \rightarrow P \rightarrow M$ process. Mathematical details are given in the Appendix. In terms of notation and relations previously described (Bogen, 1997), new assumptions used for the present study were: (1) dose rate (E) in cGy y^{-1} to surface (secretory) cells in lobar/segmental bronchi was estimated to be 3.3 and 4.4 cGy WLM^{-1} for residents and miners, respectively (NRC, 1991); (2) excess relative risk was modeled as $s \times E$ (unitless) for $S \rightarrow P$ and $P \rightarrow M$ transitions; (3) k_r was modeled as E/D_0 with D_0 taken to be the inverse-variance-weighted mean (35 cGy) of published D_0 values for alpha-induced killing of human lung cells *in vitro* (Raju *et al.*, 1993; Simmons *et al.*, 1996); (4) d_Q was modeled as $b_Q - g[1 + c(b_R b^{-1} - 1)]$; (5) $R \rightarrow Q$ and $Q \rightarrow M$ transitions were presumed to occur at a background rate per cell division of $w \times m$ (vs. the rate m assumed for $S \rightarrow P$ and $P \rightarrow M$ transitions); and (6) the target-cell turnover rate b was assumed to have the plausible value 4 y^{-1} (Bogen, 1997). Other CD2 parameters were assigned biologically plausible values previously used (Bogen,

1997) (see Appendix 1 at the end of this report).

Data Analysis. The CD2 model with 6 estimated parameters (m , w , f_R , g , c , and s) described was fit to $8 \times 6 = 48$ income-adjusted age- and exposure-specific residential LCM rates, plus $3 \times 5 = 15$ age- and WLM-bin-specific occupational LCM rates, assuming corresponding Poisson errors that were estimated by standard methods (Chiang, 1984). This model was evaluated analytically (see Appendix 1), and parameter and corresponding standard error (SE) values were obtained by inverse-variance weighted chi-square minimization (Press *et al.*, 1992) (i.e., by a method that is approximately maximum-likelihood, particularly with respect to residential LCM rates based on so many cases that assumed Poisson errors were virtually Gaussian). Outlying data were assessed by corresponding (approximate) F-tests.

The resulting fit was also compared graphically (i.e., and *not fit*) to estimates and 95% confidence-limit (CL) values for: (i) relative risk (RR) of LCM adjusted for age and income in residential WF, based on U.S. county-level mortality data discussed above; (ii) age-adjusted RR of LCM in residential WF as predicted by “preferred” BEIR VI risk-extrapolation models (NRC, 1998), (iii) RR of LCM reported by Lubin *et al.* (1994, p.88) as a function of WLM in 6 cohorts of never-smoking underground miners adjusted for age, cohort, and previous occupational exposures; and (iv) RR of LCM in 5 of the latter miner cohorts (using data discussed above) adjusted for AGE and YR, as three functions of DUR corresponding to the WLM ranges: ≤ 400 , $>400-800$, and $>800-1600$ WLM. The latter comparison involved RRs estimated *de novo* from data on 5 of 6 miner cohorts because previous studies

(Lubin *et al.*, 1995a; Lubin *et al.*, 1994; NRC, 1998) did not examine RR as a function of DUR for miners who never smoked. A >1600-WLM exposure category was not included in this comparison because CLs on the estimated (elevated) RRs were too large for a comparison to CD2 predictions to be meaningful.

For the graphical comparisons described, internally standardized RR implied by the CD2 fit (or predicted by BEIR VI models) were defined as the corresponding weighted mean of predicted age-specific RRs, using LCM numerators (i.e., inverse coefficients of variation) of age-specific 1950-54 rates of WF LCM as common age-specific weights. Comparisons between the occupational data and corresponding CD2 model predictions for LCM as functions of (i) WLM and (ii) DUR also made use of the corresponding assumptions: (i) $DUR = 9.62[1 - \exp(-0.00358 \times WLM)]$ (nonlinear least-squares fit to the 15 data subsets, $R^2 = 0.808$), and (ii) $(AGE_0/AGE) = 0.708 - 0.0122 \times DUR$ (linear least-squares fit to 27 similar subsets of the occupational data classified within three ranges of AGE, DUR and WLM cited above ($R^2 = 0.812$, $p = 1.5 \times 10^{-10}$)). Numerical maximum-likelihood methods were used to obtain all RR and CL values, as well as to obtain adjusted chi-square values for trend in the trend analyses mentioned above (Breslow and Day, 1987a). Also used in trend analyses were standardized relative-risk slopes, each defined as (adjusted LCM slope)/(unadjusted LCM intercept), with the latter slope and intercept estimated using standard methods (Fleiss, 1981). All calculations were performed using *Mathematica* 3.0[®] software (Wolfram, 1996).

2.3. Results

A separate analysis (summarized in Appendix 2) addressed potential effects of predicted intra-county variation in radon concentration on the likelihood of misclassification pertaining to the six nominal ranges of estimated annual average household radon exposure (corresponding to median radon concentrations of <0.394, 0.394-0.787, 0.787-1.38, 1.38-2.17, 2.17-3.15, and >3.15 pCi/L) that were used for the present study. This analysis showed that, despite considerable predicted intra-county variability in radon concentration, only ~1% and ~5% of houses in lowest and 2nd lowest radon bins, respectively, are predicted to have been misclassified from the highest 2 bins; and only ~2% and ~7% of houses in highest and 2nd highest radon bins, respectively, are predicted to have been misclassified from the lowest 2 bins (Price, 1999).

Table 1 summarizes results obtained from a trend analysis of LCM vs. radon-concentration bin adjusted for age and one among 21 factors considered indicate a consistent, significantly negative association between radon level and LCM, for all women as well as older women. This was also found in a similar analysis of trend adjusted for age and 210 combinations of two among the 21 other county-level factors considered, summarized in Figure 2. From the latter analysis, the median (and upper 2-tailed 95% CL) of p-values for (negative) trend obtained was 7.5×10^{-9} (0.0032) for all women (40+ y) and 4.5×10^{-7} (0.0052) for older women (60+ y). The corresponding median (and 95% CL) of relative-risk slopes was found to be -1.6 (-0.84, -2.2) L Bq⁻¹ for all women (40+ y), vs. -1.5 (-0.92, -2.1) L Bq⁻¹ for older women (60+ y). Thus, statistically significant and generally similar negative (ecologic) trends

Table 1. Trend in the relative risk (RR) of lung cancer mortality (LCM) among women in U.S. counties from 1950-54 as a function of county mean residential radon level, adjusted for various factors.*

| Adjusted for age, and | Age \geq 40 y | | | Age \geq 60 y | | |
|--------------------------|-------------------------------|---------------------|---|-------------------------------|---------------------|---|
| | RR Slope** $\times (-100)$ | CV** ($\pm\%$) | $-\text{Log}_{10} p$ for χ^2_{trend} | RR Slope** $\times (-100)$ | CV** ($\pm\%$) | $-\text{Log}_{10} p$ for χ^2_{trend} |
| Age only | 7.5 | 26 | 15. | 7.2 | 25 | 11. |
| Agr. work | 6.5 | 21 | 11. | 8.1 | 19 | 11. |
| Density | 6.6 | 21 | 12. | 6.2 | 21 | 8.4 |
| Elevation _{pw} | 3.3 | 44 | 2.8 | 3.9 | 37 | 3.1 |
| Fem. work | 6.8 | 21 | 13. | 6.4 | 21 | 8.8 |
| Heating IDD | 5.8 | 26 | 8.1 | 6.6 | 21 | 9.4 |
| High school | 8.3 | 18 | >16. | 5.9 | 25 | 6.5 |
| Income | 7.3 | 21 | 14. | 7.7 | 18 | 12. |
| Latitude | 7.9 | 21 | 15. | 7.6 | 20 | 11. |
| Migration | 6.2 | 24 | 10. | 6.8 | 21 | 9.6 |
| Poor | 7.5 | 19 | 15. | 6.2 | 24 | 8.2 |
| Precip.-h | 8.4 | 18 | >16. | 7.0 | 20 | 10. |
| Region | 8.3 | 19 | 15. | 7.9 | 19 | 13. |
| Rich | 6.9 | 20 | 13. | 6.5 | 20 | 8.8 |
| Rural | 6.6 | 20 | 12. | 6.5 | 20 | 9.0 |
| School | 8.1 | 19 | >16. | 7.7 | 19 | 12. |
| Selenium | 5.2 | 28 | 7.8 | 5.2 | 28 | 5.9 |
| Temp. Jan | 5.2 | 32 | 6.2 | 5.0 | 33 | 4.6 |
| Temp. Jul | 7.3 | 19 | 13. | 7.0 | 19 | 9.4 |
| Uneduc. | 5.1 | 31 | 6.3 | 4.9 | 32 | 4.6 |
| Urban | 6.5 | 21 | 12. | 6.2 | 20 | 8.5 |
| Wind | 8.0 | 18 | >16. | 7.6 | 18 | 12. |

Footnotes for Table 1

*LCM was compared among 6 groups of counties classified by mean residential radon level (RL), after adjusting for age and the listed factors, which were classified into U.S.-county quintiles, except as otherwise noted. Agric. work = % employed in agriculture, Density = population density (# km⁻²), Elevation_{pw} = population-weighted elevation (m), Fem. work = % females in total labor force, Heating IDD = heating infiltration degree-days (°F-d), High school = % completed high school or more, Income = median family income (\$), Migration = # persons living in a different county or abroad in 1945 vs. 1950, Poor = % with income <\$2000, Precip.-h = mean precipitation (h d⁻¹), Region = location among 9 U.S. divisions, Rich = % with income > \$5000, Rural/Urban = % rural-farm/urban population, School = median schooling completed (y), Selenium = index (0, 1, or 2) of relative exposure to dietary selenium based on foliage Se content, Temp. Jan/Jul = mean daily temperature for Jan/Jul (°F), Uneducated = % who completed grade <5, Wind = mean daily wind speed (m s⁻¹).

**The standardized RR slope (B_{adj}) was calculated as $B_{adj} = b_{adj}/a$, where b_{adj} = the adjusted slope for linear LCM trend, and a = the unadjusted LCM intercept; CV = 100%×(standard deviation of B_{adj})/ B_{adj} .

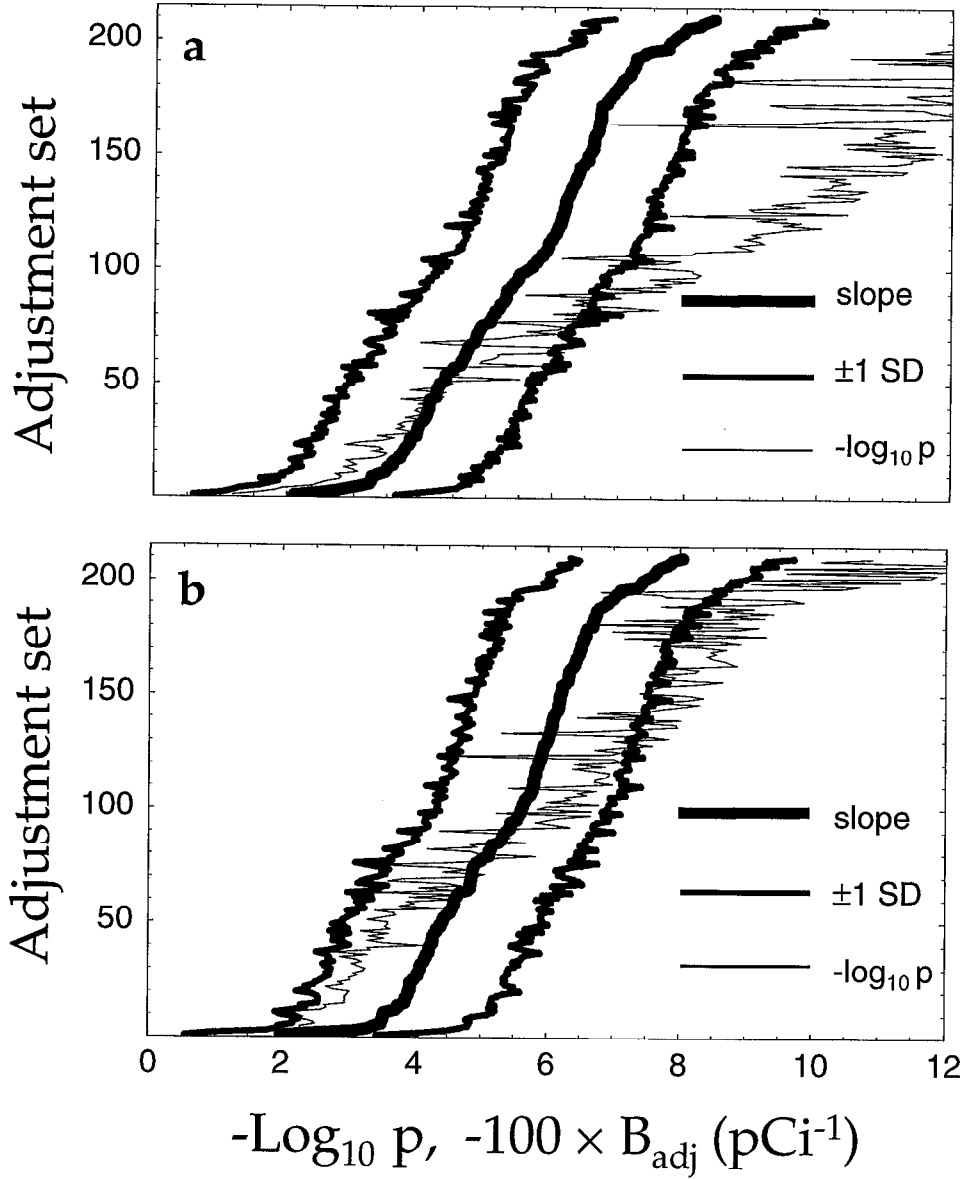


Figure 2. Adjusted relative-risk slopes and corresponding p-values for adjusted trend in 210 analyses adjusting for age and two additional variates (among those listed in Table 1) are shown for U.S. females **(a)** 40+, and **(b)** 60+, years of age. Cumulative distributions of normalized adjusted slope (B_{adj}) are surrounded by corresponding lower and upper (± 1 SD) bounds; corresponding p-values plotted as $(-\log_{10} p)^{-1}$ for corresponding adjusted tests of trend are overlaid. Slope values refer to linear trend in relative-risk of lung cancer mortality (LCM) in U.S. females during 1950-54, for county data pooled within 6 ranges of estimated annual average household radon exposure, with slope calculated as $B_{adj} = b_{adj}/a$ where b_{adj} = the adjusted LCM slope and a = the unadjusted LCM intercept.

for LCM vs. radon were observed using either data on all women (40+ y) or data pertaining only to older women (60+ y).

An adequate CD2 fit was obtained to the combined ($n = 63$) age-specific residential/miner LCM data ($\chi^2 = 73.8$, $df=57$, $p = 0.066$), which was improved significantly ($F_{2,55} = 9.72$, $p = 0.00024$) by dropping one outlying data point from each data subset ($\chi^2 = 54.6$, $df=55$, $p = 0.49$). Parameter estimates ($\pm 100\% \times SE/estimate$) corresponding to the latter CD2 fit were: $mb = 0.76 \times 10^{-8} \text{ y}^{-1} (\pm 12\%)$, $w = 3.7 (\pm 27\%)$, $f_R = 0.063 (\pm 50\%)$, $g = 0.0893 \text{ y}^{-1} (\pm 4.9\%)$, $c = 0.35 (\pm 65\%)$, and $s = 0.11 \text{ y cGy}^{-1} (\pm 160\%)$.

Figure 3 shows the corresponding CD2 fit obtained to income-adjusted age-specific data on LCM in U.S. WF in 1950-54 for two of the six county-mean household radon levels considered. RR values predicted by this CD2 fit under residential-exposure assumptions are compared in Figure 4a to: (i) corresponding RR estimates that summarize LCM in U.S. WF in 1950-54 as a function of county-mean residential radon level, and (ii) corresponding RR values predicted by “preferred” BEIR VI models (NRC, 1998). Figure 4b shows how, under mining-exposure assumptions reflecting the actual experience of nonsmoking miners, the CD2-model predicts RRs consistent with those summarizing the age-specific miner data used. Figure 5 shows how, under similar assumptions concerning nonsmoking miners, the CD2-model predicts RRs consistent with “inverse dose-rate” effects on RR apparent in miners, even though the model was not fit to any data concerning inverse dose-rate effects.

2.4. Discussion

The similarity in trend-analysis results obtained using age-specific 1950-54 data

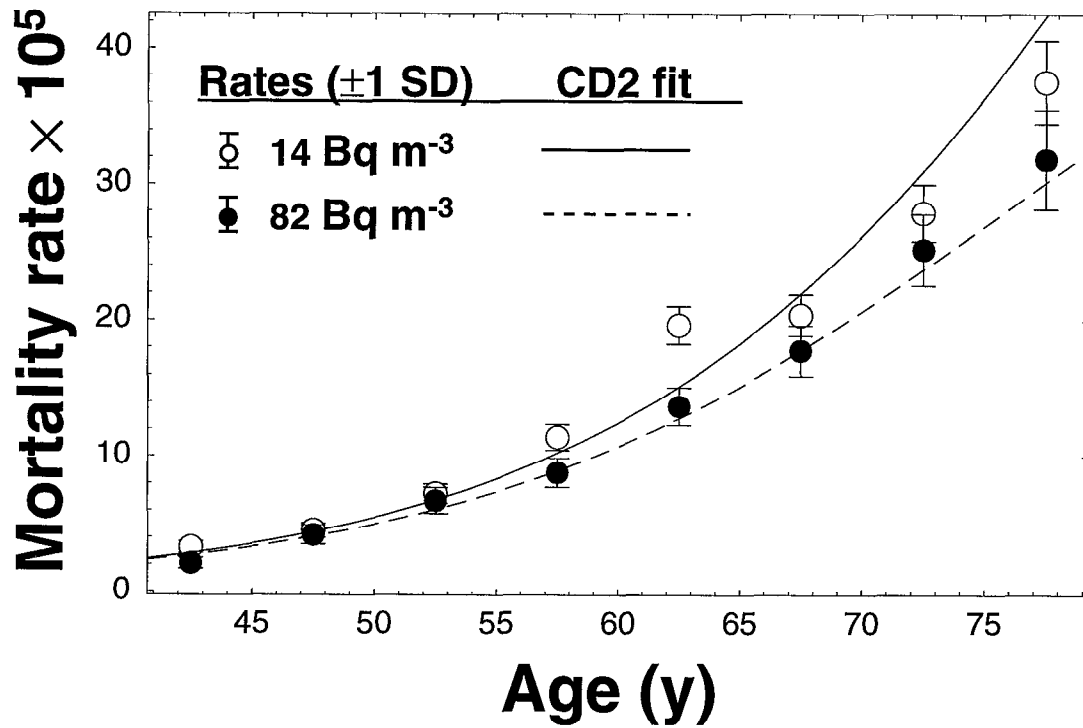


Figure 3. Age-specific rates of lung cancer mortality (LCM) in U.S. white females during 1950-54 adjusted for income, pertaining to counties within 2 different ranges of county-mean residential radon concentration. The LCM data are compared to age-specific LCM rates predicted by the 6-parameter CD2 model fit *jointly* to: (i) the data points shown, (ii) similar U.S. county-level data for 4 other ranges of county-mean residential radon, and (iii) age-specific LCM rates for a total of 2,488 miners who never smoked (goodness of fit to combined data: $\chi^2 = 54.6$, $df=55$, $p = 0.49$).

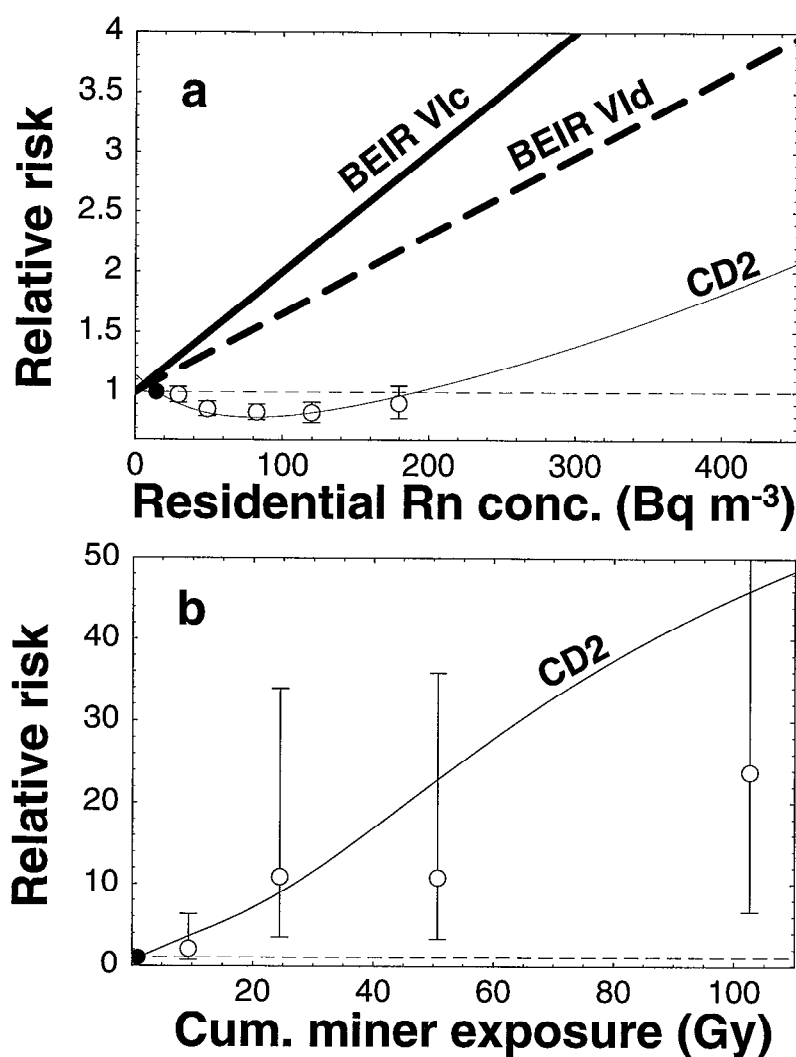


Figure 4. Relative risk (RR) of increased lung cancer mortality (LCM) in (a) U.S. white females (WF) during 1950-54, adjusted for age and income, vs. county-mean residential radon concentration within 6 ranges; and (b) 2,488 nonsmoking underground miners adjusted for age, cohort, and previous occupational exposures, vs. cumulative underground mining exposure as reported by Lubin et al. (1994). Each set of RR estimates was based on internal comparisons to data (solid points) corresponding to the lowest exposure group (RR = 1, dashed line), and is compared to RRs predicted by the 6-parameter CD2 model fit to 61 age-specific LCM rates for WF and nonsmoking miners (see Figure 3) corresponding to the RR estimates shown. Plot (a) also shows RR for female nonsmokers predicted by the “preferred” (12- and 13-parameter) BEIR VI linear-extrapolation models: BEIR VIc = age-exposure-concentration model, BEIR VIId = age-exposure-duration model (NRC, 1998).

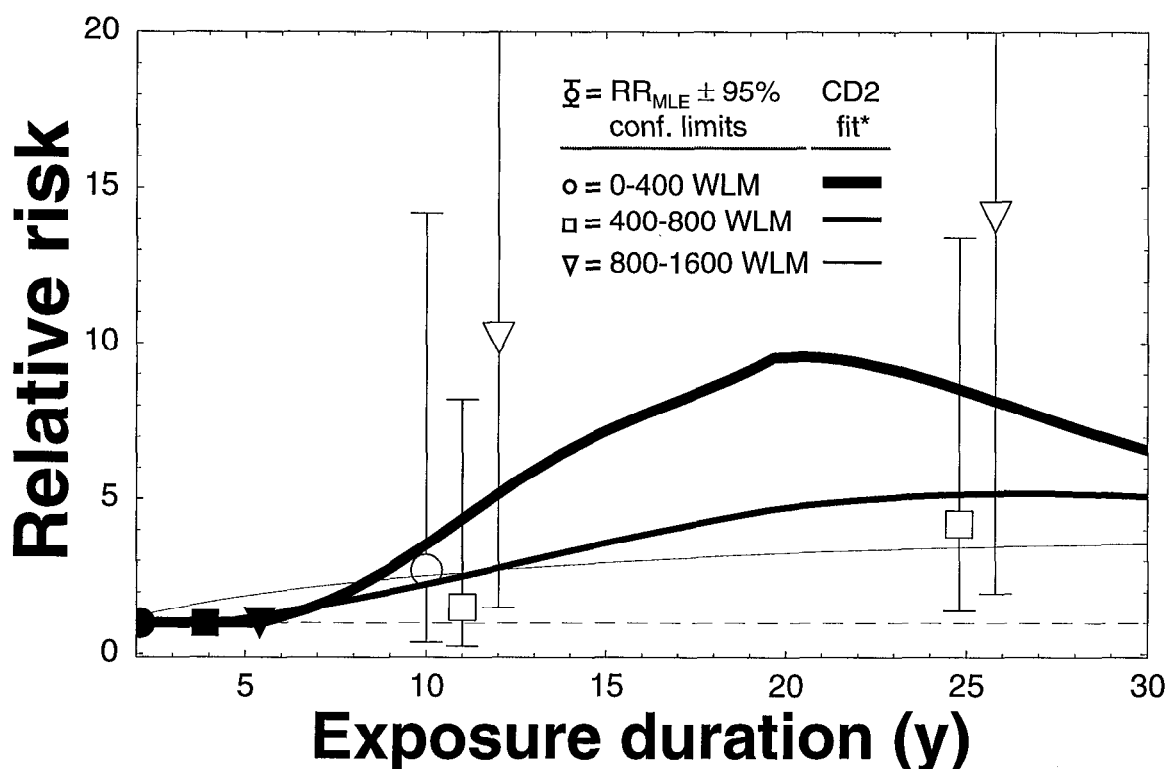


Figure 5. Relative risk (RR) of increased lung cancer mortality (LCM) adjusted for age and year of observation in nonsmoking underground miners within different categories of cumulative exposure, vs. mining-exposure duration; based on internal comparison to LCM in miners exposed for <8 y (solid points on dashed line indicating RR = 1). The RR estimates are compared to values predicted by the 6-parameter CD2 model fit—not to the data points shown here—but rather to 61 age-specific LCM rates for 1950-54 WF and nonsmoking miners (see Figure 2).

on Lcm in U.S. women of age 40+ vs. 60+, despite far less smoking among the older women, indicates that inter-county confounding by smoking is unlikely to explain the apparent negative trend in age-specific data on LCM vs. residential radon. As noted (Introduction), these negative trends may be due entirely or in part to a confounding artifact due to within-county correlations unaffected by the various county-level adjustments made in this study (Lubin, 1998; Pershagen, 1998; Smith *et al.*, 1998). The results above indicate, however, that these negative trends are also consistent with a biologically realistic six-parameter CD2 model that also predicts high-dose as well as dose-rate effects in miners. In particular, CD2 estimates obtained for *bm* and *bmw* ($\sim 10^{-8} \text{ y}^{-1}$) are consistent with *in vivo* somatic *hpgrt*-gene-mutation rates estimated for human T-lymphocytes, which in turn have been used to estimate somatic human-oncogene mutation rates (King *et al.*, 1994; Mendelsohn, 1990; Robinson *et al.*, 1994; Trainor *et al.*, 1984). The CD2 estimate for f_R ($\sim 6\%$) is consistent with relevant histological and microdosimetric variabilities, and/or with a possible source of unexposed bronchial-epithelium stem cells within underlying submucosal-gland ciliated ducts—see the detailed discussion and references cited in Appendix 1 of Bogen (1997).

In conclusion, the results of this study support the biological plausibility of the hypothesis long argued by Cohen (Cohen, 1995), that LCM is not increased by exposure to radon at residential levels. More specifically, they are consistent with a mechanistically based U-shaped (or “hormetic”) dose-response pattern for radon’s effect on lung-cancer risk, but by no means prove that this pattern either is the case or is as large as suggested by the U.S. ecologic data considered. The U-shaped CD2 fit

obtained in this study differs sharply from linear-no-threshold models, such as the 12- or 13-parameter “BEIR VI” (NRC, 1998) models currently used to extrapolate lung-cancer risks for low-level radon exposures (Figure 4). The present study thus indicates that some consideration of fundamental model uncertainty ought to play a role in risk management for residential radon (Bogen and Layton, 1998).

Furthermore, the results obtained pose testable mechanistic hypotheses concerning the effect of subchronic or chronic exposure to relatively cytotoxic genotoxins, such as alpha radiation, on growth kinetics of premalignant foci. After chronic administration of chemical carcinogens, development of focal cytotoxic resistance in proliferative foci has been attributed to clonal selection for mutations that decrease chemical uptake, decrease metabolic activation, increase deactivation, increase excretion, increase DNA repair, etc. (Emmelot and Scherer, 1980; Last *et al.*, 1987). Even so, chronic chemical carcinogen exposures have been shown to reduce tumor yields significantly under some conditions (Kociba, 1978; Witschi *et al.*, 1997). In the case of radon, one underlying CD2 hypothesis is that premalignant foci are no more resistant than surrounding normal cells to chronic alpha-induced cell death. Focal resistance is not expected in the case of alpha radiation, because a fraction of the damage (e.g., multiple chromosome breaks) induced is predictably misrepaired to states that are at least reproductively lethal.

Another key CD2 hypothesis is that cell proliferation induced to compensate for normal-cell loss from low-level alpha exposure is not accompanied by the same amount of (or any) increased proliferation in surface-epithelial (*P*-cell) premalignant foci. At low levels of induced target-cell killing, the CD2 model used posits that: (i)

this low level of chronic cell killing is too low to induce fully compensatory cell proliferation, and/or (ii) focal cells (already assumed to have an elevated rate of proliferation—see Appendix) are either less responsive or totally unresponsive to mitogenic signals that induce regenerative proliferation in surrounding normal cells. The second of these assumptions is supported by the observation that magnitudes of relatively increased mitotic rates in foci compared to normal rat liver cells are characteristic of particular focal types (Zerban *et al.*, 1994). Experiments that address this issue directly, which have yet to be done, may thus provide data critical to improved risk prediction for low-level exposures to those carcinogens, like alpha radiation, expected to be similarly cytotoxic to both normal and premalignant cells.

Improved risk extrapolation for residential radon exposures will, of course, ultimately rely on large, well designed case-control and cohort studies. Previous non-ecologic epidemiological studies have yielded mixed results, generally consistent with low-dose linearity, but also insufficiently powerful and not well designed to test specific nonlinear hypotheses (Bogen, 1997; Lubin *et al.*, 1995b; NRC, 1998; Samet, 1989; Stidley and Samet, 1993). Better predictions will require detailed exposure histories and lung-cancer data concerning tens of thousands of people (Lubin *et al.*, 1995b). A coordinated effort to generate a database of large magnitude is now underway in Europe, Canada and the U.S. Initial results indicate a relative-risk pattern that is nearly linear for some data sets (e.g., those focusing on areas of relatively high residential exposure—(Darby *et al.*, 1998; Pershagen, 1998)), but flat or possibly U-shaped for other data sets (e.g., those focusing on combined low and high residential-exposure areas, or on nonsmokers—(Alavanja *et al.*, 1994; Létourneau *et*

al., 1994; Pershagen, 1998; Wichmann *et al.*, 1998)). The degree of nonlinearity predicted by the CD2 model is a sensitive function of the ratio of cytotoxic to mutagenic potencies assumed (Bogen, 1997). However, the key assumption behind this predicted nonlinearity—alpha-induced killing of premalignant cells in bronchial-surface epithelium—is highly likely. Some (albeit perhaps negligible) nonlinearity in lung-cancer risk due to residential radon is thus predicted by current, mechanistically based multistage cancer theory. If properly designed, future analyses of expanded sets of residential case-control data will bound the magnitude and significance of such nonlinearity.

3. Historical U.S. Residential Fuel Use and Female Lung Cancer Mortality

[coauthored by J. Cullen and Dr. K.T. Bogen]

3.1 Background

U.S. female lung cancer mortality increased dramatically during the 20th century. Cigarette smoking patterns, movement into industrial occupations and outdoor air pollution have been associated with this increase (Chen *et al.*, 1992). However, despite early century female domestication, residential air pollution has not been thoroughly examined in relation to these historical mortality patterns.

Increasing attention has focused on the relation between residential fuel combustion and lung disease, particularly in China where cooking and heating with coal and wood is still a common practice (Band *et al.*, 1990; Chapman *et al.*, 1988; Chen *et al.*, 1990; He *et al.*, 1991; Liu *et al.*, 1991,1993; Mumford *et al.*, 1987,1989; Qing *et al.*, 1993; Xu *et al.*, 1986,1989), as summarized in Table 2. Ecological studies have shown exceptionally high female lung cancer mortality rates in Northern China despite an estimated 0.2% female smoking prevalence (Band *et al.*, 1990; Chapman *et al.*, 1988; Chen *et al.*, 1992; He *et al.*, 1991; Liu *et al.*, 1991; Mumford *et al.*, 1987,1989; Xu *et al.*, 1989). Case-control studies have also shown a strong association between residential coal use and female lung cancer mortality in Northern China (Chen *et al.*, 1990; Gao *et al.*, 1987; Liu *et al.*, 1993; Liu *et al.*, 1989,1991). Other putative risk factors, such as passive smoking and occupation, do not account for the exceptionally high lung cancer mortality among these women (Band *et al.*, 1990; Chapman *et al.*, 1988; Mumford *et al.*, 1987,1989). Historically, occupational studies of coal mining and lung cancer have been inconclusive, showing both elevated and reduced disease rates associated with mining (Ames *et al.*, 1983; Armstrong *et al.*, 1979; Bertrand *et al.*, 1987; Chovil, 1979; Cockcroft and Andersson, 1987; Costello *et al.*,

Table 2. Association of residential coal use with increased lung cancer risk in chinese regions.

| Study design* | Study size (Cases/Contr.) | Exposure type | Exposure level | Risk measure* | Est. | p value (or CI)* | Reference |
|---------------|---------------------------|---|--|-------------------|--------------------------|---|-------------------------|
| Ecol. | 11 Communes | Smoky coal use (%) | 0% 50% 100% | PRR | 1.0 15.4 217 | NP | Chen et al. 1990 |
| CC | (1249/1345) | Use vs. non-use (y) of: central gas coal stove open coal bed coal bed | 30+ vs. 0 50+ vs. 0 20+ vs. 0 50+ vs. 0 | RR _{adj} | 0.8 1.2 2.3 3.4 | NS NS <0.05 <0.05 | Morabia et al. 1992 |
| CC | (110/426) | Female cooking (y) | 30-44 vs. <30 >44 vs. <30 | OR | 7.23 8.43 | <0.05 NS | Wu-Williams et al. 1993 |
| CC | (139/139) | Smoky coal use Net tons smoky coal used per y | Yes/No <3 vs. 0 >3 vs. 0 | OR _{adj} | 7.53 8.24 7.53 | (3.31-17.2) (2.33-29.2) (3.03-18.7) <0.001 (trend) | Xu et al. 1989 |
| CS | 117,035 PY | Males: Coal vs. gas use | — | RR SRR | 1.44 1.45 | NP NP | Gao et al. 1987 |

*PRR = prevalence rate ratio, RR = relative risk, OR = odds ratio, CC = case control, CS = cross-sectional, Ecol. = ecological, LCM = lung cancer mortality. RR_{adj} = RR adjusted for age, education, smoking; OR_{adj} = OR adjusted for age, menstrual-cycle duration, menopause, age, family chronic-bronchitis/LC history; CI-confidence interval.

1974; Dalal *et al.*, 1991; Gustavsson *et al.*, 1988; IARC, 1997; Levin *et al.*, 1988; Lyon *et al.*, 1981; Meijers *et al.*, 1988,1991; Minowa *et al.*, 1988; Morabia *et al.*, 1992; Une *et al.*, 1995; Wu-Williams *et al.*, 1993). However, lack of data on individual smoking behavior may have obscured results in some of these studies (Lyon *et al.*, 1981; Meijers *et al.*, 1988; Minowa *et al.*, 1988). Importantly, a lower cancer potency of coal-mine dust versus coal particles of incomplete combustion (PIC) might be expected based on the greater concentrations of mutagenic compounds in the former (IARC, 1997).

Of three Northern Chinese residential fuel types, only “smoky” coal has been linked to increased lung cancer mortality; neither “smokeless” coal nor wood fuel were associated with any significant effect (Band *et al.*, 1990; Chapman *et al.*, 1988; de Koning and Smith, 1984; Mumford *et al.*, 1987,1989,1990). Smoky coal is comparable to U.S. medium-volatile bituminous coal of low sulfur content, whereas smokeless coal is more similar to hard coal such as lignite or anthracite (Mumford *et al.*, 1987,1989). Despite heavy soot residue left by smoky coal, its use in China may have persisted due to its ability to rapidly generate large amounts of heat, as measured in British thermal units (Btu). PIC from smoky or bituminous coal are associated with elevated lung cancer mortality in laboratory animals (Liang *et al.*, 1988; Pott and Stöber, 1983). When burned, smoky coal emits higher levels of sub-micron organic PIC versus wood or smokeless coal, which are mutagenic in Ames Salmonella bioassays (Mumford *et al.*, 1987,1990). Lung cancer has been induced in mice exposed to coal smoke and skin cancer development has occurred in mice treated topically with filtered organic coal extracts.(Mumford *et al.*, 1990) Polycyclic aromatic hydrocarbon (PAH) components of PIC, such as benzo(a)pyrene, dibenzo(a,l)pyrene, and 7,12-dimethylbenz(a)anthracene are effective experimental and

suspected human carcinogens (Chuang *et al.*, 1992; Cupitt *et al.*, 1994; de Koning and Smith, 1984; Higginbotham *et al.*, 1993; Mumford *et al.*, 1989). Elevated PAH-DNA adducts and urinary PAH levels have been associated with residential smoky coal (He *et al.*, 1991; Mumford *et al.*, 1993,1995).

Cooking and heating fuels are among sources of residential air pollution. Until the 1950's, coal and wood were the predominant fuels burned in U.S. homes (USBC, 1953). Perhaps due to steady replacement by natural gas and electricity, few studies have examined the public health impact of coal and wood combustion in U.S. homes (Lambert, 1997; Samet *et al.*, 1987,1988; USBC, 1953). Indoor wood smoke has been linked to several respiratory illnesses, while indoor coal smoke has been measured in U.S. homes but not studied in association with human health (Yocom *et al.*, 1971; Cooper, 1980; de Koning and Smith, 1984; Dennis *et al.*, 1996; Honicky *et al.*, 1985; Liang *et al.*, 1988; Marbury, 1991; Mumford *et al.*, 1989; Robin *et al.*, 1996; Tuthill, 1984).

This ecological analysis examined the relation of U.S. domestic bituminous coal consumption to age-specific lung cancer mortality (LCM) in U.S. white females dying during 1950-54, the great majority of whom never smoked (particularly those ≥ 60 years old). A comparative analysis of these rates within different age ranges (40+ vs. 60+) provided a way to assess the potential confounding effect of inter-county differences in (rather low) smoking prevalence on any association observed between LCM and coal use, as explained below. Socio-demographic, climatic, and geophysical covariates were also examined. The present study is the first nationwide evaluation of a relationship between coal use and lung cancer in the U.S.

3.2. Materials and Methods

County-level LCM data for the states AL and HI were unavailable, in the case of VA included unreliable mortality rates, and for the major retirement states (CA, AZ, and FL) corresponded to a relatively low percent (<70%) of lifetime residence within 25 miles of that at the time of death compared to other states (Cohen, 1992b; Marsh *et al.*, 1996). Therefore, a total of 2,821 counties were considered in this analysis, including those in AK, AZ, CA, FL, HI and VA (as in Section 2). Because socioeconomic status and other demographic covariates may influence indoor air pollution exposure (Lebowitz, 1983), adjustment was performed on several demographic factors for which U.S. county-level data could be obtained as classified below.

Lung Cancer Mortality Data. U.S. county-level mortality rates (deaths per person-year) were obtained for lung cancer (bronchus, trachea, + lung; ICDA 162-163, 6th Revision) during 1950-54 in white females by 5-year age intervals (Marsh *et al.*, 1996). Due to the rarity of female lung cancer at that time, particularly in younger age groups, data on women under age 40 were excluded and age-specific data were combined into 10-year age intervals (40-49, 50-59, 60-69, 70-79, 80+).

Analyses were carried out for all women (40+ years) and also for women aged 60+. The latter restriction addressed potential (inter-county) confounding due to cigarette smoking insofar as smoking prevalence in 1950-54 among U.S. white females aged 60+ vs. 40+ was approximately 5% vs. approximately 11%, respectively, and women aged 60+ smoked fewer cigarettes and started smoking at a later age than women aged 40+ (Garfinkel, 1981; Haenszel and Shimkin, 1956; Haenszel *et al.*, 1956). Based on these historical smoking data, excess risk for elevated LCM in white women dying at age 40+

(vs. 60+) in 1950-54 was estimated to be 0.74 (vs. 0.16) for women aged 40+ (vs. 60+) compared to expected LCM risks for never-smoking women who died during this period. This estimated 4- to 5-fold difference in excess risk indicates that any ecological association observed between indoor BC use and female LCM due solely to inter-county confounding by smoking should be greatly reduced in analyses involving older women (aged 60+) compared to those involving all women considered (aged 40+).

Coal Data. The number and percent of homes using coal for (central + non-central) heating in 1940 were obtained from U.S. census data (USBC, 1943). Because Mumford demonstrated that “smoky” or bituminous coal, and not anthracite or “smokeless” coal, is associated with increased female LCM, our study focused on domestic BC consumption *per se* within counties that used mainly coal for heating (Mumford *et al.*, 1987,1989). County-level data for the year 1918 on domestic *per capita* net tons of BC consumption (fuel utilization in housing units/residences, apartment buildings, and small local businesses) were obtained from a detailed map published by the U.S. Fuel Administration (Leshner, 1919). Similarly detailed data could not be obtained for other years. Binned quartiles of 1918 BC consumption were used as an index of residential coal exposure to coal smoke in our analysis. The LCM data used were based on deaths among all residents of a county, but not all persons living in U.S. counties burned coal. We therefore focused specifically on counties in which a substantial fraction of homes burned coal as fuel by restricting the analysis to counties in which $\geq 75\%$ of homes used coal for heating.

Females dying between 1950-54 reached ages 29-33 (the approximate midpoint of their lives) by 1918, which is the year of the coal-use data considered in the present

analysis. To examine the potential impact any changes in net tons BC consumed (NTBCP) *per capita* between 1918 and 1940, county-level consumption for nine U.S. regions in 1918 was compared to corresponding 1940 U.S. regional summary data on average tons of BC consumed per dwelling unit (TBCD) (Bituminous Coal Institute, 1948). To convert from TBCD to NTBCP, regional 1940 populations were divided by dwelling units per region in 1940, weighted by the fraction of 1940/1950 regional populations, with removal of states not considered (as discussed). The 1918 NTBCP data were also weighted as a fraction of the 1950 population for direct comparison to 1940 TBCD. Regions were subsequently categorized into two groups based on whether BC use in 1940 was $<$ or was ≥ 1 NTBCP; the two groups had a mean (± 1 SDM) BC use level of 0.89 (± 0.036) and 1.9 (± 0.053) NTBCP, respectively. This BC-use category was used as an additional adjustment variable in our analysis, to examine the potential effect of different patterns of change in BC use subsequent to 1918, at least at a regional level.

Demographic Data. Census data on the following 1950 county-level socio-demographic variables were obtained: total population, population density, U.S. region (among nine regions considered), urban population, rural-farm population, educational level (total years), income (median family income), migration (number of persons living in different county or abroad in 1949 vs. 1950), females in the workforce (%), and persons employed in agriculture (%); income grouped as rich ($\% \geq \$5,000$ income) vs. poor ($\% < \$2,000$ income); and educational level dichotomized as uneducated ($\% < \text{grade } 5$) vs. highly educated ($\% \geq \text{high school}$) (USBC, 1953). These socio-demographic variables were evaluated as corresponding county quintile values, using 1950 county populations as weights.

Geophysical and Nutrient Data. Respiratory exposure to radon is associated with increased lung cancer risk in animals and underground miners, and so was included as an adjustment variable (Bogen, 1997,1998; NRC, 1988). Clinical trials and prospective studies have indicated that dietary selenium intake may be protective against cancer development at specific sites, including the lung (Blot *et al.*, 1993; van den Brandt *et al.*, 1993). Additionally, climatic factors which might influence indoor coal smoke concentration were included for adjustment. Geophysical variates considered at the U.S. county-level were: annual average residential radon estimates; a 3-level index of dietary selenium exposure based on corresponding data on selenium content in local foliage; and five 1953-75 “typical” climatic measures, including daily hours of precipitation, January/July temperatures, wind speed, and heating infiltration degree days or “heating IDD” which correlates with energy use for home heating (Apte *et al.*, 1997; Clark *et al.*, 1991; Price *et al.*, 1998). Residential radon estimates used for this purpose were derived from county-specific U.S. Environmental Protection Agency survey data, adjusted for additional geophysical and climatic factors using Monte Carlo and regression techniques (Price *et al.*, 1998).

Statistical Analysis. Adjusted relative risk (RR) estimates and confidence intervals were calculated using maximum-likelihood estimation, and corresponding adjusted chi-square tests for trend were performed (Breslow and Day, 1987b). RR estimates were computed using a standardized slope, B_{adj} (in units of inverse *per capita* net tons of BC used), where $B_{adj} = b_{adj}/a$, and where b_{adj} (the adjusted LCM slope) and a (the unadjusted LCM intercept) were estimated by standard methods (Fleiss, 1981). Standard deviation

(SD) and coefficient of variation (CV) estimates for B were obtained assuming approximate lognormality of b_{adj} and a .

Socio-demographic and geophysical variables were used for adjustment in combination with age separately for each age range (40+ vs. 60+), creating: 20 2-variate analyses (involving age with or without one other variable), and 190 3-variate analyses (involving age and two other variables) (Table 3). Fisher's chi-square test was used to determine the overall significance of p-values for adjusted trend obtained for each set of multiple tests conducted (Fisher, 1973). All statistical calculations were performed using Mathematica 3.0 software (Wolfram, 1996).

3.3 Results

Approximately 640 (22.7%) of the 2,821 U.S. counties in 1940 were characterized by 75% or more homes heated by coal. Women aged 40+ in "high coal-using" counties experienced an estimated 5,807 female LC deaths within 46,120,369 person-years (PY) of observation versus 4,059 LC deaths among 16,887,421 PY of observation for women aged 60+. Across all counties for both age groups, a total of 14,296 LC deaths occurred in 113,999,028 PY during the period of interest. Quartiles of BC consumption across high coal-using counties were 0.03, 0.45, 1.4, and 2.4 net tons, from lowest to highest quartile, respectively.

Adjusted slope (B_{adj}) and trend-test p-values for the two-variate analyses (age and one other variate) are summarized in Table 2 for all women (aged 40+) and for older women (aged 60+). All adjustment combinations yielded significant statistics indicating a positive trend, and the estimated slopes for all women (aged 40+) were similarly distributed to those for older women (aged 60+).

Table 3. Trend in Relative risk (RR) of 1950-54 female lung cancer mortality (LCM) among U.S. counties in which $\geq 75\%$ of homes used coal for heating.*

| Adjusted for age and: | Age ≥ 40 y | | | Age ≥ 60 y | | |
|-----------------------|-----------------------------|---------------------|---|-----------------------------|---------------------|---|
| | Slope** ($\times 100$) | CV** ($\pm\%$) | -Log ₁₀ p for χ^2_{trend} | Slope** ($\times 100$) | CV** ($\pm\%$) | -Log ₁₀ p for χ^2_{trend} |
| Age only | 9.8 | 38 | 7.2 | 9.2 | 27 | 4.2 |
| Agriculture | 9.3 | 28 | 6.5 | 9.9 | 27 | 5.0 |
| Density | 9.4 | 26 | 6.6 | 9.9 | 23 | 5.0 |
| Female work | 7.9 | 31 | 4.6 | 9.2 | 27 | 4.2 |
| Heating IDD | 11.0 | 30 | 8.5 | 11.0 | 31 | 6.0 |
| High school | 11.0 | 30 | 6.3 | 10.0 | 31 | 4.2 |
| Income | 7.6 | 32 | 4.2 | 8.1 | 30 | 3.3 |
| Migration | 11.0 | 25 | 9.3 | 12.0 | 25 | 6.8 |
| Poor | 8.3 | 28 | 5.0 | 8.9 | 27 | 4.0 |
| PrecipHr | 9.3 | 33 | 6.2 | 10.0 | 32 | 5.1 |
| Region | 17.0 | 20 | 12 | 16.0 | 22 | 7.7 |
| Rich | 6.9 | 38 | 3.4 | 7.7 | 35 | 2.9 |
| Rn | 7.2 | 35 | 3.6 | 7.7 | 34 | 2.8 |
| Rural | 8.6 | 29 | 5.7 | 9.4 | 27 | 4.5 |
| School | 8.4 | 40 | 4.9 | 9.4 | 38 | 4.1 |
| SeBin | 10.0 | 31 | 7.7 | 11.0 | 32 | 5.6 |
| TempJan | 11.0 | 27 | 8.7 | 11.0 | 26 | 6.4 |
| TempJul | 9.3 | 31 | 6.3 | 10.0 | 30 | 5.0 |
| Uneduc | 9.0 | 30 | 5.9 | 10.0 | 26 | 5.0 |
| Urban | 7.8 | 32 | 4.5 | 8.7 | 30 | 3.8 |
| Wind | 7.3 | 44 | 3.4 | 6.5 | 53 | 2.0 |

*LCM was compared among 4 groups of counties classified by annual per capita BC use (net tons), after adjusting for the following factors (each classified into U.S.-county quintiles unless specified otherwise): AgWork = % employed in agriculture, Density = persons/km², FemWork = % females in total labor force, Heating IDD = heating infiltration degree-days, High school = % completed high school or more, Income = median family income, Migration = # persons who lived in different county or abroad in 1949 vs. 1950, Poor = % with income < \$2000, PrecipHr = daily hours of precipitation, Region = location within 9 U.S. divisions, Rich = % with income > \$5000, Rural = rural farm population, School = median school years completed, SeBin = index (0, 1, or 2) of relative exposure to dietary selenium, TempJan/TempJul = daily mean temperature for indicated month, Uneducated = % who completed < grade 5, Urban = urban population, Wind = mean daily wind speed.

**Slope = normalized RR slope (B) = (factor-adjusted slope of LCM as a linear function of BC, by person-year-weighted regression)/(unadjusted intercept of corresponding linear fit); CV = 100% \times (SD_{slope}/Slope); see Materials and Methods.

Results of the three-variate analyses (age and two other variates) for all women (aged 40+) and older women (aged 60+) are summarized in Figure 6 by corresponding cumulative distributions of B_{adj} , plotted together with corresponding lower and upper (± 1 SD) bounds on B_{adj} and (-log inverse) p-values for adjusted tests of trend. The p-values distributions in Figure 6 indicate that significant trends were obtained for almost all three-variate adjustment combinations. Comparing highest vs. lowest BC-use quartile among women aged 40+, simultaneous adjustment for wind and region with age showed the most significant LCM/BC-use relationship for three-variate analyses, with $RR_{adj} = 1.68$ (1.28, 2.21) and $p < 10^{-9}$ for adjusted trend while simultaneous adjustment for region and age from two-variate analyses resulted in the most significant LCM/BC-use association, with $RR = 1.54$ (1.25, 1.9) and $p < 10^{-13}$ for adjusted trend. Similar findings for women aged 60+ were obtained for these variable combinations. The percent of p-values ≥ 0.05 was 3% for women aged 40+ and 6% for women aged 60+, i.e. no greater than might be expected by chance. Fisher χ^2 values for the overall significance of the sets of 190 p-values obtained for three-variate analyses involving 40+ and 60+ women were highly significant ($\chi^2 = 4490.5$ and $p \approx 0$ for 40+, $\chi^2 = 3363.7$ and $p \approx 0$ for 60+).

Adjustment for BC use in 1918 vs. 1940 produced similarly significant results when two- and three-variate analyses were repeated.

3.4 Discussion

Overall, BC consumption in 1918 was shown to be significantly associated with female LCM in 1950-54 for counties of high coal use after statistical adjustment for numerous combinations of variates (Table 3, Figure 6). Importantly, this significant positive LCM-BC association was observed in two female age groups, 40+ and 60+, whose

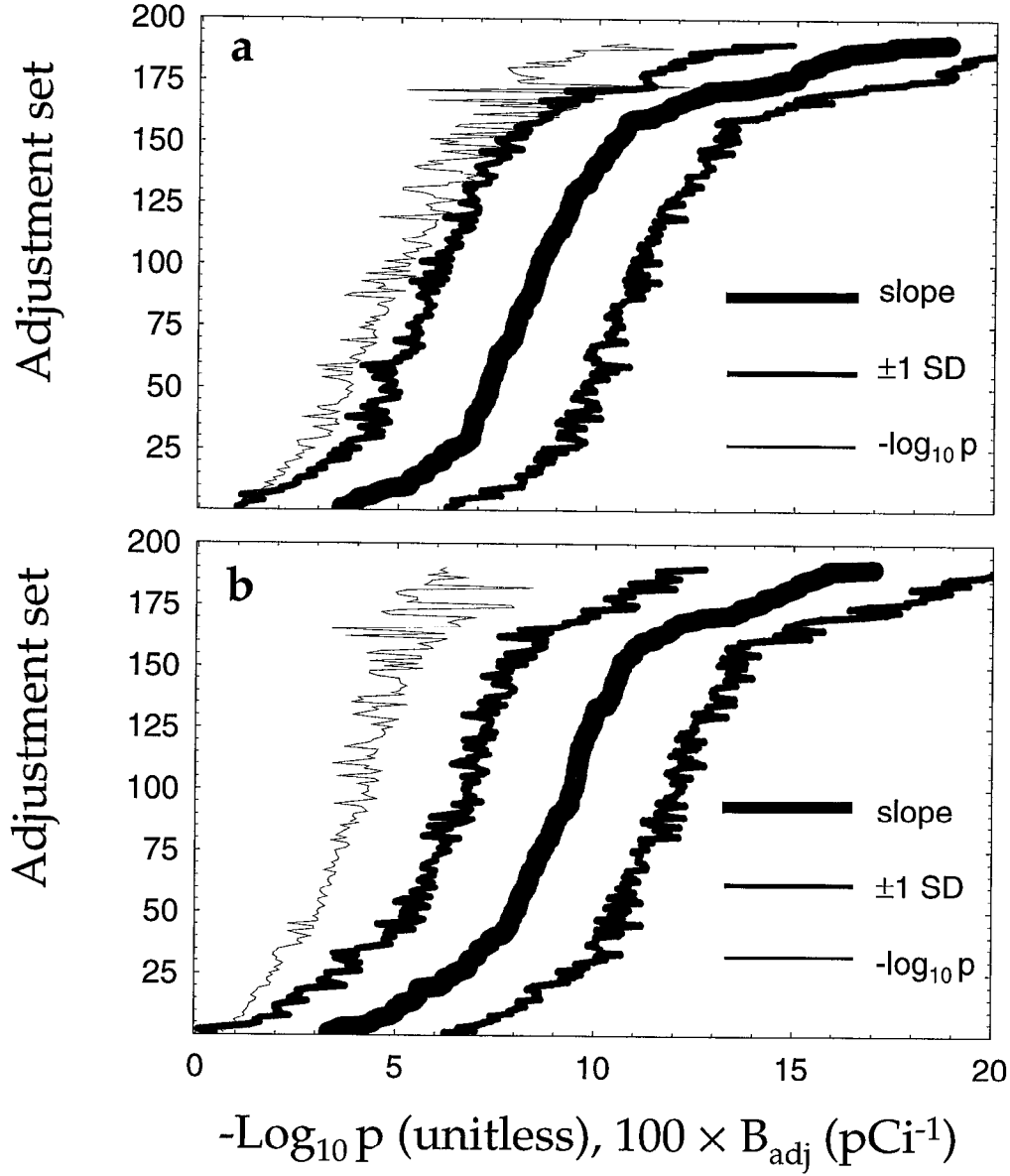


Figure 6. Adjusted relative-risk slopes and corresponding p-values for adjusted trend in 190 analyses adjusting for age and two additional variates, (among those listed in Table 3) are shown for U.S. females (a) 40+, and (b) 60+, years of age. Cumulative distributions of normalized adjusted slope (B_{adj}) are surrounded by corresponding lower and upper (± 1 SD) bounds; corresponding p-values plotted as $(-\log_{10} p)^{-1}$ for adjusted tests of trend are overlaid. Slope values refer to relative risk of lung cancer mortality (LCM) based on comparisons of highest (>2.4 net tons) vs. lowest (≤ 0.03 net tons) county quartiles of bituminous coal use, with slope calculated as $B_{adj} = b_{adj}/a$ where b_{adj} = the adjusted LCM slope and a = the unadjusted LCM intercept.

1955 smoking prevalence (approximately 11% and 5%) differed markedly (Haenszel and Shimkin, 1956; Haenszel *et al.*, 1956), which is consistent with the hypothesis that confounding by smoking is unlikely to explain the observed association.

Inherent limitations of the ecological study design (Greenland, 1992; Greenland and Morgenstern, 1989; Greenland and Robins, 1994; Piantadosi, 1994; Piantadosi *et al.*, 1988) are countered by several unique features of the present study. The wide investigative scope achieved from evaluating 640 U.S. counties of high coal use was a major strength. Cigarette smoking, the most significant risk factor for lung cancer, was addressed by performing a restricted analysis with women aged 60+, who smoked roughly half as much as all women combined (40+). While intra-county associations between low-prevalence smoking and coal use cannot be ruled out as explaining the observed association between BC use and female LCM, the consistency of the observed effect among women aged 40+ vs. 60+ indicates that the BC-LCM association is not likely due to inter-county confounding by cigarette smoking.

Because of concern over the constancy of BC use during the lifetime of women dying in 1950-54, the LCM-BC relationship was compared regionally in 1940 vs. 1918. Similar findings after adjustment for regional BC use patterns of 1940 indicate that this relationship does not appear to be attributable to changes in geographic patterns of BC use between 1918 and 1940.

Burning rate of fuel, type of stove, and coal rank have all been shown to impact the amount of indoor pollution generated (McCrillis and Burnet, 1990; Mumford *et al.*, 1989; Mumford *et al.*, 1987). While burning rate and stove-type data were not available, our focus on consumption of bituminous coal was intended to address this matter.

Additionally, insofar as home ventilation is an important aspect of indoor air pollution, heating IDD was used to examine any potential effect of home energy use that would typically correlate with reduced home ventilation and greater indoor air pollutant concentration.

4. Effect of Radon Exposure on Liver Foci in Japanese Medaka: An Experimental Test of CD2-Model Predictions

4.1 Background

Experimental work conducted as part of this LDRD-sponsored project culminated a collaboration with Mark Okihira, D.V.M., Ph.D., and Professor David Hinton at the University of California, Davis (U.C. Davis), School of Veterinary Medicine. These experimental work involved subchronic exposure of three groups of 148 Japanese medaka fish (rice-fish minnows) to different aqueous concentrations of radon gas. The purpose of the study was to examine effects of alpha exposure (arising from the decay of radon, which partitions into fish livers at a concentration proportional to that of radon in tank water) on the occurrence and growth of premalignant cells (namely, enzymatically altered proliferative “foci”) in the livers of young fish exposed subchronically to different concentrations of radon gas. Specifically, the study was conducted to test the CD2-based hypothesis that alpha exposure should increase the frequency but retard the growth of liver foci. Fish liver foci were studied because: many fish can be exposed and studied economically, proliferative foci in liver (as opposed to most other tissues) can be identified and

examined by staining techniques, the response of liver foci in Japanese medaka to chemical carcinogens has been studied for decades.

4.2 Materials and Methods

Three weeks after the medaka were hatched at U.C. Davis, the fish were all “initiated” to increase the naturally low, spontaneous occurrence of liver foci in these fish to larger, more easily detected frequencies. Initiation was done by exposing them for 1 hour to a 500-ppm concentration of the direct-acting mutagen and liver carcinogen, diethylnitrosamine (DEN). Four weeks later at LLNL, the fish were separated into three specially modified 80-liter fish tanks: a control tank, and two tanks with water containing elevated concentrations of radon gas, derived from a 10-mCi radium source through which 100 to 500 mL/min of dry air was directed. To maintain different radon concentrations in tank water, air containing a background level, a low, or a higher radon concentration was sparged continuously into the corresponding tank water throughout the exposure period. Dried room air was used to dilute radon-enriched air from the radium source. All tanks were located within a single hood, illuminated from above with three 30-inch Vita-Glow® fluorescent lamps operated using a 12-h light/dark cycle.

Each tank was sealed on top using air-tight fittings, and kept filled with between 70 and 72 liters of purified, reconstituted water (Recon) optimized for medaka growth, which was maintained at 25 ± 1 °C and pH = 7.6. Each tank included a thermostat, and one biofilter drawing air from the tank headspace; after the sixth week of exposure identical submerged power filters and sintered-glass bacterial

matrices were added to each tank to enhance biofiltration efficiency. From 10 to 20% of the water from each tank was replaced with fresh Recon once per week. Sparge and biofilter air were circulated (with a combined flow rate of ~ 70 mL/min) through each tank by an air-flow control unit adjacent to the hood containing the tanks; the unit also directed samples of sparge and biofilter air from each tank to two corresponding RD-200 monitors that measured corresponding radon+daughter activity in air sampled for 30 min from each source on a continually rotating basis. A tank-air outflow of ~ 30 mL/min, equal to the sparge air inflow, was released from a small port on each tank into the hood. Tank water was sampled periodically by gas-tight syringe through a small port to monitor pH and radon, nitrite, nitrate, oxygen, and ammonia concentrations. Fish were manually fed pre-weighed amounts (totaling $\sim 5\%$ of body weight per day) of fine-grade UCD-prepared medaka food, dispensed 2 to 4 times/day.

After 10 weeks of exposure, 40 fish were harvested from each tank, and all remaining fish were sacrificed 4 weeks later. After sacrifice, each fish was weighed and its liver was excised, fixed in formalin, and prepared for sectioning into slides for histological examination and quantitative morphometry of liver foci.

A separate experiment was conducted after the 14-week radon exposure to measure the equilibrium tissue:water partition coefficient for radon gas partitioned between tank water and soft (relatively rapidly perfused) medaka tissue. In this experiment, 111 fish were maintained for 48 h in a large nylon net within the sealed high-concentration tank containing an approximate mean radon concentration of 40,000 pCi/L over that period. Over a period of ~ 1 min, these netted fish were then

removed from the tank, drained, blotted dry on tissue paper, rinsed in a 10-L bucket of Recon, and (still contained within a small portion of netting cut from the original netting) finally placed into a 4-L Nalgene jar pre-filled with 3.5 L of Recon. The jar was then sealed with a screw cap including fittings allowing 500 mL/min of dry air to be bubbled into the bottom of the jar, with air collected at the top directed into one of the RD-200 counters mentioned above for a period of 1.5 h, after which the fish were euthanized and weighed.

Counts from jar air measured over a 60-min period were compared to counts measured in one subsequent and two previous control experiments, before and after each of which the 4-L jar was thoroughly rinsed with Recon and the air lines were purged until no counts above background were detected. The two previous control experiments involved measuring counts for 60 min after direct injection of 10 mL of water from the tank from which the 111 fish (weighing a total of 19.9 g) were removed shortly thereafter. In the subsequent control experiment, the same small piece of netting used to place the 111 fish into the 4-L jar was placed back into the sealed tank from which the fish were taken, allowed to re-equilibrate with radon in tank water for 15 min, and then placed into the pre-filled jar for measuring released radon as before. Counts measured from the jar containing fish plus netting, less those measured from the jar containing just the netting, were compared to those measured after injection of 10 mL of tank water to determine the amount of radon removed from the fish compared with that contained in tank water.

4.3 Results

From the separate experiment conducted after the 14-week radon exposure, was determined that, at equilibrium, radon is about 1.5- to 3-fold more concentrated in rapidly perfused medaka tissue than in surrounding tank water. About 16% of all the fish exposed over 10 to 14 weeks died prior to sacrifice; mortalities occurred more often in the low-concentration tank, compared to the control and high-concentration tanks. The examination of fish livers is currently being completed at U.C. Davis.

5. Conclusions

In conclusion, modeling results from this LDRD study support the biological plausibility of the hypothesis that LCM is not increased by exposure to radon at residential levels. They are consistent with a mechanistically based U-shaped (or “hormesis”) dose-response pattern for radon’s effect on lung-cancer risk, but by no means prove that this pattern either is the case or is as large as suggested by the U.S. ecologic data considered. The U-shaped CD2 fit obtained as described in Section 2 differs sharply from linear-no-threshold models currently used to extrapolate lung-cancer risks for low-level radon exposures. The analysis described in Section 3 supports the hypothesis that ecologic data meaningfully contributed to the CD2-fit to residential and occupational radon-vs.-LCM data described in Section 2, insofar as the same ecologic data reveal a significant positive association between lifetime

bituminous (smoky) coal use and LCM in U.S. women during 1950-54, in agreement with both ecologic and case-control studies on LCM vs. coal use among women in China. The present study thus indicates that some consideration of fundamental model uncertainty ought to play a more important role in risk management for residential radon (Bogen and Layton, 1998). Furthermore, the results obtained pose testable mechanistic hypotheses concerning the effect of subchronic or chronic exposure to relatively cytotoxic genotoxins, such as alpha radiation, on growth kinetics of premalignant foci. One such test, described in Section 4 above, is being completed as part of this study.

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Appendix 1

Mathematical Details of the CD2 Model

Mathematical details of the CD2 model applied to radon are presented below, proceeding from the summary description and notation in Figure 1 and Methods. (Note: dependence of variables on time t is occasionally suppressed for convenience.) Rates b_T and d_T (y^{-1}) denote mean birth and death/differentiation rates, respectively, for cell type $T = S, D, P, R$, or Q . It was assumed that $(b_P/b_S) = (b_Q/b_R) = n = 10$, based on values of ~ 5 to 20 reported in studies comparing growth kinetics in proliferative foci and surrounding normal tissues (Barrass *et al.*, 1993; Dragan *et al.*, 1994; Rotstein *et al.*, 1986; Zerban *et al.*, 1994). For non-cytotoxic conditions, it was assumed that: the rate g (y^{-1}) governs net growth of P - and Q -cell foci (i.e., $b_P - d_P = b_Q - d_Q = g$), $b_S = b(1 - f_R)$, $b_R = d_S = b$, and $d_R \ll b$ (i.e., $d_R \approx 0$), where b^{-1} (y) is the mean R -cell turnover time. The rate $b = 4 y^{-1}$ was assumed for normal human segmental bronchial epithelium, consistent with the range of values measured in normal tracheobronchial epithelial cells of rats and hamsters (Bertalanffy, 1968; Boren and Paradise, 1978; Kauffman, 1980; Reid and Jones, 1983) and values used for purposes of human radon dosimetry (Fisher *et al.*, 1991; Hofmann *et al.*, 1991).

The rate k_r (y^{-1}) of induced reproductive death was modeled as E/D_0 , with D_0 taken to be the inverse-variance-weighted mean (35 cGy) of published D_0 values for alpha-induced killing of human lung cells *in vitro* (Raju *et al.*, 1993; Simmons *et al.*, 1996). Mutation rates m_T (y^{-1}) were modeled as $b_T m_i (1 + sE)$ or $b_T m_i' (1 + sE)$, where the corresponding mean background mutation rates per cell division, m_i and m_i' ($i=1$ for $T=S$ or R , $i=2$ for $T=P$ or Q , prime only for $T=R$ or Q), were estimated in terms of (unitless) parameters m and w under assumptions that $m_1 = m_2 = m$ and $m_1' = m_2' = w m$. Alpha-induced interphase (as opposed to reproductive) cell death was not modeled explicitly. Tumors were assumed to be lethal at time $t + \tau$ conditional

on $M(t) \geq 1$, where tumor latency τ was assumed to be 5 y, consistent with the range of values used in previous radon-related studies (Darby *et al.*, 1995; Hornung and Meinhardt, 1987; Moolgavkar *et al.*, 1993; NRC, 1988,1998; Whittemore and McMillan, 1983). Cytodynamic relations among S , D , and R cells were assumed to be governed by a deterministic, Verhulst feedback-inhibition submodel that specifies how b_R increases to ensure that $S(t)+D(t)$ tends toward $S(0) = S_0$, under the assumptions that D cells are “recognized” by R cells as normal S cells, and that $R(t) = R(0) = R_0 = f_R S_0$ for all t (i.e., that the increases in b_R to offset R -cell losses are virtually “instantaneous” on the time scale considered). It was assumed that $S_0 = 10^8$ cells, based on estimates of basal vs. secretory cell populations in human lung (Harley, 1988; Mercer *et al.*, 1991);

Equations (1)-(14) below give the corresponding birth and death rates specifying the CD2 model applied to radon in this study:

$$b_S = b(1-f_R) \quad (1)$$

$$d_S = b + k_r \quad (2)$$

$$b_D = 0 \text{ (by definition)} \quad (3)$$

$$d_D = b(2-f_R) \quad (4)$$

$$b_R = b + G(t) \quad (5)$$

$$b_P = n b_S \quad (6)$$

$$d_P = b_P - (g + k_r) \quad (7)$$

$$b_Q = n b \quad (8)$$

$$d_Q = b_Q - g[1 + c(b_R b^{-1} - 1)] , \quad (9)$$

where $G(t)$ is defined by the Verhulst relations:

$$G(t) = G(\infty) + a\{1 - ([S(t)+D(t)]/S_0)\} \quad (10)$$

$$dS(t)/dt = (b + G(t))f_R S_0 + (b_S - d_S)S(t) \quad (11)$$

$$dD(t)/dt = k_r S(t) + (b_D - d_D)D(t) . \quad (12)$$

The constant c (unitless) in Eq. (9) reflects an assumption that (unexposed basal) premalignant stem (Q) cells respond to regenerative mitogenic signals via a death-

rate decrease proportional to the increase in R -cell birth rate over its normal value, b . The parameter a (y^{-1}) in Eq. (10) governs the speed of S -cell replacement, and was assumed to be sufficiently large to justify the assumption used that $S(t)|E \approx S(\infty)$, where for sequential exposures E_i during time intervals $\{t_{i-1}, t_i\}$, $S(t)$ is interpreted as $S_i(t-t_{i-1})$ such that $S_i(0) = S_{i-1}(\infty)$ and $S_0(\infty) = S_0$, and where analogous relations were presumed for D . Consequently, after substituting Eqs. (1-4) into Eqs. (10-12) and some algebra, it follows that

$$G(\infty) = \left[\frac{S(\infty)}{S_0} \left(b - \frac{k_r}{f_R} \right) \right] - b = \left[\frac{1}{1 + k_r [b(2 - f_R)]^{-1}} \left(b - \frac{k_r}{f_R} \right) \right] - b \quad (13)$$

The CD2 model described was evaluated using the analytic solution to the 2-stage stochastic (MVK) model with piecewise-constant parameters, which during each i th interval (using his notation) involves corresponding rates of mean occurrence (v_i), birth (β_i), death (δ_i), and mutation (μ_i) of premalignant cells (Zheng, 1995). Dropping the i -subscript, the latter three rates correspond directly to the rates b_P , d_P , and m_P , or to the rates b_Q , d_Q , and m_Q , as defined above. The expressions used for v in the $S \rightarrow P \rightarrow M$ and $R \rightarrow Q \rightarrow M$ processes were fS_0m_P and $f_RS_0m_Q$, respectively. The corresponding process-specific hazard functions, $H_S(t)$ and $H_R(t)$, were presumed independent and each calculated as described by Zheng (1995). The latter independence implies that the age-specific hazard function for the 6-parameter CD2 model described is simply $H(t) = H_S(t) + H_R(t)$. From the fact that a single MVK-type hazard function with at most three piecewise-constant parameters is identifiable (Heidenreich *et al.*, 1997), it follows directly that the 6-parameter CD2 model described is also identifiable in theory.

[Note: References cited in this Appendix appear above in the Reference Section of this report.]

Appendix 2

Estimated distributions of county GSDs of indoor radon concentrations

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by Dr. Phillip Price

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Estimated distribution of county GSDs of indoor radon concentrations.

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1 Introduction

A long-standing goal of the radon research community has been to produce maps that somehow identify areas of elevated radon (e.g. Gundersen et al. 1993, Price et al. 1997, Cohen 1994, Alexander et al. 1993), where “elevated radon” is often somewhat vaguely defined but may include the arithmetic mean long-term indoor concentration in the area, or the geometric mean, or the fraction of homes exceeding some reference level such as the EPA’s recommended action level of 4 picoCuries per liter (pCi/L). The intent of such maps is often to identify areas for increased radon education, monitoring, and remediation, but sometimes radon maps (or, more generally, estimated radon distributions by area) are used for other purposes such as epidemiological modeling (Bogen 1997, Lubin and Steindorf 1995, Cohen 1995) or for analyzing costs and benefits of radon monitoring strategies (Lin et al, 1999).

Indoor radon measurements within counties are nearly lognormally distributed, so most quantitative predictions of radon distributions attempt to determine the geometric mean (GM) and geometric standard deviation (GSD) of measurements by county. Observed GSDs tend not to be highly variable compared to the GMs, and variables that are predictive of GMs have not been found to help predict GSDs; consequently, it is common to assume that county GSDs are identical, or that they only vary slightly. However, there is a possibility that some counties have unusually elevated GSDs, and thus have a large fraction of high-radon homes even if their GM concentrations are fairly low. Knowledge of the distribution of county GSDs is thus necessary in order to determine the effectiveness of mean-based

radon mapping methods.

Furthermore, predicted radon-related cancer rates in nonlinear radiation-risk models depend not only on arithmetic mean concentrations, but also on the distribution of radon exposures across the population (Bogen 1997), so variation in GSDs is a potentially important complicating factor in fitting such models. For example, a model that attempts to predict county lung cancer death rates as a function of indoor radon concentration, and that assumes that the entire county population is exposed to the county’s arithmetic mean concentration, will substantially misclassify many or most individuals in the county. An example is presented in Appendix I, where we consider the number of households whose radon concentration falls into various concentration range bins, as a function of the county arithmetic mean, for several values of county GSD.

A complication in characterizing the radon distribution within counties is that most radon measurements are short-term measurements, usually made on the lowest level of the home (often an unoccupied basement). Such measurements are known as “screening” measurements, and they are both biased and “noisy” compared to annual-average living-area measurements. The bias can be removed, given presently available short- and long-term data (White et al. 1990, Price and Nero 1996), but the existing data are not adequate for precisely estimating the excess variability of short-term measurements. Moreover, such excess variability probably varies by season and location. In short, there is no known way to use the variability of screening measurements within areas (such as counties) to estimate the variability of long-term living-area concentrations.

However, there is one high-quality database of long-term living-area radon measurements that is suitable for quantifying the within-county variation of indoor radon concentrations: the National Residential Radon Survey (NRRS) made radon measurements in about 5700 homes selected through a stratified random sampling scheme that sampled a total of 125 counties across the U.S. (Lucas et al. 1992). In this paper, we present the results from fitting these data with a statistical model that estimates both the within-county and within-census-block variation of indoor radon concentrations, and also quantifies the extent to which the variability itself varies among counties and census blocks.

2 The Data

The NRRS protocol used an alpha-track radon detector on every occupied level of the house, with a measurement time of 1 year, to calculate a “household mean” radon concentration—the arithmetic mean of the radon measurements on all occupied levels. Weighting by occupancy time was not used, so that if 80% of the inhabitants’ time was spent on one level of the home, while only 20% was spent on another level, the household mean measurement does not reflect this disparity. Still, this is the only large-scale random-sample survey that monitored on every occupied level of the home, and as such it is certainly the best survey for estimating parameters related to actual indoor exposures.

The survey also recorded a large variety of features of each home, such as the number of appliances vented to the outdoors, the type of heating and cooling system, and so on. Although such information has been used to produce predictive radon models, we do not use it in the present work, which is involved in characterizing radon distributions rather than in trying to locate high- or low-radon areas.

An important complicating factor in the survey is that a stratification scheme was used to oversample expected high-radon areas; furthermore, population weighting was used so that highly populous counties were more likely to be selected than sparsely populated ones. Sampling weights were calculated as part of the original survey.

2.1 Components of variation

The NRRS selected 125 counties through a stratified random sampling scheme. Within each county, exactly eight census blocks were selected (also via a stratified sampling scheme), and a small number of homes was selected in each block. The survey attempted to monitor every one of those homes.

The stratification scheme must be considered when estimating the GSDs and their uncertainties, since there is the possibility of missing very variable (or very uniform) census blocks within a county, and since only eight census blocks are sampled within each county so that inclusion of one census block with very high (or low) GM may also affect the estimated GSD. To get a feel for the magnitude of the components of variability, we plot observed radon measurements in Figure 1 for eight of the counties in EPA’s Region III (the mid-Atlantic states). Each thin vertical column contains the measurements from one census

block, and the blocks are divided into their counties by the vertical bars. Measurements are plotted on a log scale using a number identifying the county (using the ‘primary sampling unit’ identifier from the NRRS data). Note that some census blocks are more variable than others within the same county (particularly noticeable in the rightmost county). This illustrates that some census blocks are more variable than others (in log space).

In county 26 (sixth from the left) most of the census blocks have about the same mean radon level, whereas in county 25 (seventh from the left) there appears to be substantial variation. This illustrates that some counties have higher between-census-block variation than others (in log space).

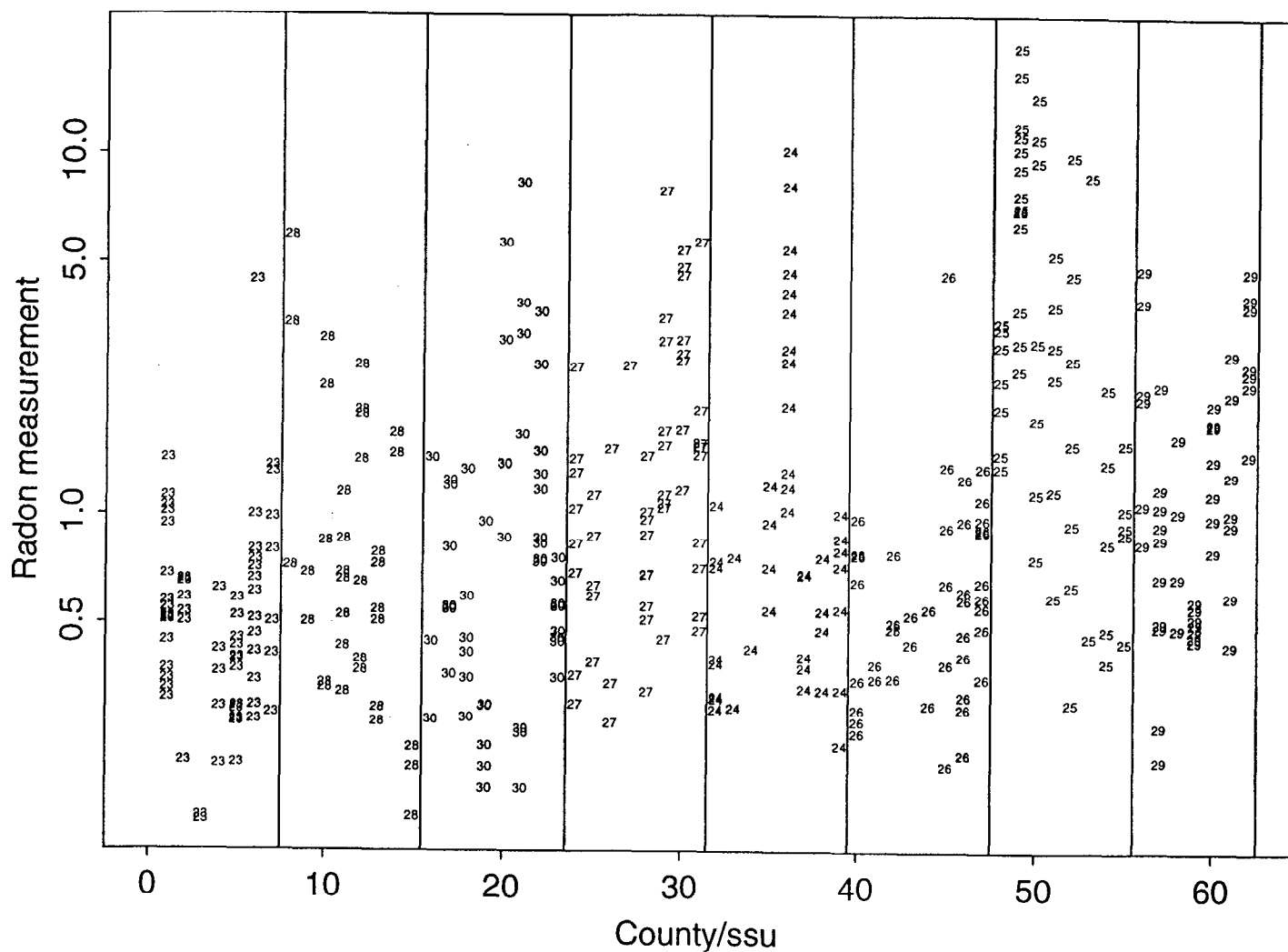
It is apparent, given the large variation within census blocks and the small number of observations in each block, that the parameters associated with any individual census block can only be poorly estimated. Indeed, even the county parameters are not well estimated from these data—for example, county 24 (fifth from the left) has one sampled census block with much higher radon measurements than the others in the county, containing about 1/4 of the measurements in the county. Are 1/4 of the homes in the county really that high, or is it even higher, or much lower? Small-sample noise obviously creates substantial uncertainty in the parameters describing individual counties, although this uncertainty can be captured with an appropriate statistical model.

2.2 Sensitivity to measurement error.

Like all measurements, the alpha-track radon measurements were subject to error. Of particular concern for the present study is the effect of background subtraction on the GSD estimates by county. Background subtraction is necessary because even unexposed alpha-track detectors show some damage that is interpreted as raw counts of radiation exposure. To remove this spurious effect, an expected number of background counts is subtracted from the observed radon count for the detectors. However, random variation ensures that sometimes this expected background level will overestimate the actual background, while at other times it will underestimate it. In cases where the actual radon concentration is quite low, subtracting an overestimate of the background count can lead to a physically impossible (and meaningless) negative radon measurement. Moreover, because of the “regression effect”, most of the very low radon measurements (say, less than 0.3 pCi/L household mean concentration) are underestimates of the true annual-average concentration. The influence

Figure 1. "Flyspeck" plot of observed radon measurements in eight counties in Region III (the mid-Atlantic states). Each wide vertical bin contains the data from one county. Within each county, a different column contains the data from a census block. Each point (plotted by a number indicating the county, using the identifier in the NRRS data) represents the radon measurement in a home. The y axis is logarithmic.

Some census blocks are much more variable than others; e.g., see county 29 (the last column)---one census block has very little variation in measurements compared to the others..



of the background subtraction effect diminishes with higher radon concentrations, since the effect is of the order of ± 0.1 pCi/L, which becomes a trivial adjustment for measurements over 1 or 1.5 pCi/L.

Still, when estimating the GSDs (by county, or by census block) it is necessary to handle the extremely low measurements somehow. Discarding them altogether is statistically invalid, since they really do represent homes with low radon levels. For calculating GMs and GSDs of observed data, one can use the maximum likelihood method with an appropriate lower limit of 0.2 or 0.3 pCi/L, but the results can still depend on where this lower limit is set; additionally, such a method is inconsistent with complete modelling of the radon distribution. A better approach would be to include the background subtraction effect in the model, but the model would then be vastly more complicated.

In this work, we apply a slight adjustment to the radon measurements: we replace each radon measurement r with $r' = r/2 + \sqrt{r^2/4 + D}$, with $D = 0.15$ pCi/L. This transformation has little effect on values of r above about 0.5 or 0.75 pCi/L (leading to transformed values of 0.54 and 0.78 pCi/L, respectively), but yields transformed radon concentrations above 0 in all cases; moreover, the resulting distribution of transformed radon measurements within each region is nearly lognormal. However, this equation is merely a convenient ad hoc adjustment, and does not necessarily bring the measurements into line with reality.

Unfortunately, the results in the present paper are somewhat sensitive to the details of this procedure, most notably in regions with many very low household mean radon measurements: Regions 1, 6, 9, and 10, in all of which 18% or more of the reported measurements are less than 0.3 pCi/L. For example, in one of the census blocks in Region 1 (New England), 3 of the 5 reported mean concentrations are below 0.3 pCi/L, although none are below 0.1. The sampling GSD of the observed data is 2.08, but the GSD of the transformed data (transformed as above) is 1.48, and if $D=0.1$ pCi/L were used as the adjustment rather than 0.15 pCi/L, then the GSD of the transformed data would be 1.62.

In short, given the shortcomings of the data it is difficult to estimate the actual GSDs for areas in which many of the radon measurements are very low.

3 The Model

3.1 Model definition

The NRRS data are stratified, and this stratification must be accounted for in estimating the county GSDs. After some preliminary investigations, it was clear that a realistic statistical model of the NRRS measurements must include several components of variation: the individual-house measurements are more variable in some census blocks than in others, and the census block GMs more variable in some counties than in others.

Let y_{ijk} be the log measurement in home k , in census block j of county i . We will denote the vector of $\{y_{ij}\}$ values with y , and likewise will denote the vector of any of the following parameters by dropping the subscripts.

We assume that the house-to-house variance within a census block, δ_{ij}^2 , varies from one census block to the next:

$$y_{ijk} \sim N(\theta_i + \phi_{ij}, \delta_{ij}^2) \quad (1)$$

where θ_i is the county effect for county i and ϕ_{ij} is the census block effect for block j in county i .

We further assume that the county effects are normally distributed about some grand mean μ :

$$\theta_k \sim N(\mu, \tau^2), \quad (2)$$

and that the census block effects are normally distributed about zero, with the variance in census block effect itself varying among counties:

$$\phi_{ij} \sim N(0, \sigma_i^2). \quad (3)$$

We further assume that the variances are drawn from distributions

$$\sigma_{ij}^2 \sim \text{Inv-}\chi^2(\nu_\sigma, \sigma_0^2) \quad (4)$$

and

$$\delta_{ij}^2 \sim \text{Inv-}\chi^2(\nu_\delta, \delta_0^2), \quad (5)$$

with $1/\nu_\sigma$ and $1/\nu_\delta$ given flat (uniform) prior distributions from 0 to infinity.

3.2 Fitting the model

The model was fit with a combination of alternating conditional sampling (also known as the Gibbs Sampler) and Metropolis Monte Carlo methods, as described in Gelman et al. (1995).

Ignoring the Metropolis steps for the moment, the Gibbs Sampler holds all of the parameters fixed except for one, and draws a candidate value of that parameter from the sampling distribution conditional on the values of all of the other parameters (plus the data). Thus it is necessary to work out the conditional distribution of each parameter, given the other parameters and the data. For notational simplicity, we introduce notation so that γ represents the entire set of data and parameters in the model: $\{y\}, \mu, \tau, \{\sigma\}, \{\phi\}, \{\delta\}, \nu_\sigma, \nu_\delta, \sigma_0, \delta_0$, with a bracketed symbol following γ denoting all of the parameters *except* the subscripted one. The resulting equations for each parameter are (from application of Bayes's theorem): For the county and block effects,

$$\phi_{ij}|\gamma[\phi] \sim N\left(\frac{\sum_k (y_{ijk} - \theta_i)/\delta_{ij}^2}{1/\sigma_i^2 + n_{ij}/\delta_{ij}^2}, \frac{1}{1/\sigma_i^2 + n_{ij}/\delta_{ij}^2}\right), \quad (6)$$

and

$$\theta_i|\gamma[\theta] \sim N\left(\frac{\mu/\tau^2 + \sum_j n_{ij}(\bar{y} - \phi_{ij})/\delta_{ij}^2}{1/\tau^2 + \sum_j n_{ij}/\delta_{ij}^2}, \frac{1}{1/\tau^2 + \sum_j n_{ij}/\delta_{ij}^2}\right) \quad (7)$$

The conditional distributions of δ_{ij}^2 and σ_i^2 are scaled-inverse- χ^2 :

$$\delta_{ij}^2|\gamma[\delta] \sim \text{Inv-}\chi^2\left(\nu_\delta + n_{ij}, \frac{\nu_\delta \delta_0 + \sum_k y_{ijk} - (\theta_i + \phi_{ij})}{\nu_\delta + n_{ij}}\right) \quad (8)$$

and

$$\sigma_i^2|\gamma[\sigma] \sim \text{Inv-}\chi^2\left(\nu_\sigma + np_i, \frac{\nu_\sigma \sigma_0^2 + \sum_j \phi_{ij}}{\nu_\sigma + np_i}\right) \quad (9)$$

where np_i is the number of secondary sampling units in county i .

Finally, the distributions of δ_0 and σ_0 are Gamma:

$$\sigma_0|\gamma[\sigma_0] \sim \Gamma\left(\frac{n_\theta \nu_\sigma}{2} + 1, \sum_i \frac{\nu_\sigma \text{igma}}{2\sigma_i^2}\right) \quad (10)$$

and

$$\delta_0|\gamma[\delta_0] \sim \Gamma\left(\frac{n_\delta n_{u\delta}}{2} + 1, \sum_{ij} \frac{n_{u\delta}}{2\delta_{ij}^2}\right). \quad (11)$$

Note that the model defined above does take account of the stratification structure of the data, but does not include the over- and under-sampling of some areas. Taking account

of the stratification would be necessary if we were analyzing GMs, but investigation (using both ordinary and Bayesian regressions) shows no correlation between GSDs and sampling weights, although there *is* a correlation between GMs and sampling weights). Areas that were more likely to be sampled have neither higher nor lower GSDs than areas that were less likely to be sampled.

4 Results

Before discussing the results, we caution the reader that an unusual amount of attention is required in order to understand what is being said in this section. Recall that the overall goal is *not* to try to characterize the within-county variability of radon (that is, we are *not* trying to estimate a GSD within a county), rather we are trying to characterize the *distribution* of GSDs, or to put it another way, to characterize the variability of the within-county variability. Already this can be confusing, but we are also compelled to discuss the uncertainty in the distribution of variabilities. This presents some challenge in terms of clarity of exposition.

Starting from the most understandable level: the results of the analysis do include estimates (and uncertainties) of the variances for each of the individual census blocks and counties in the NRRS data; however, as these constitute a total of only 125 of the 3000 U.S. counties, and only eight of the census blocks within each county, these particular parameters are not particularly informative. More importantly, the analysis estimates the so-called “hyperparameters” describing the overall distribution of variances between census blocks and between homes within census blocks. The situation is somewhat analogous to using the NRRS data to estimate the distribution of household radon concentrations in the U.S.—the geometric mean, geometric standard deviation, etc., can be determined for the whole U.S. and for individual regions, but this knowledge does not tell us which U.S. counties have elevated or depressed radon levels. Similarly, the present analysis tells us the distribution of county GSDs, but does not tell us which GSDs are high and which are low (except for those included in the data, of course).

Table 4 shows central parameter estimates for each region. The Monte Carlo method used to estimate the parameters generates many estimates (we used 8000 Monte Carlo steps) for each parameter; the table shows the median value of the hyperparameters describing the within-county variability, as well as the implied 50% range of county GSD’s. For instance,

Table 1: Central estimates of parameter values, by region.

| Region | median | median | median | median | est. percentiles of GSD dist. | | | | |
|--------|--------------|--------------|--------------|--------------|-------------------------------|------|------|------|------|
| | σ_0^2 | ν_σ | δ_0^2 | ν_δ | 10 | 25 | 50 | 75 | 90 |
| I | 0.453 | 29 | 0.500 | 31 | 2.53 | 2.61 | 2.71 | 2.82 | 2.95 |
| II | 0.288 | 34 | 0.401 | 17 | 2.28 | 2.32 | 2.38 | 2.45 | 2.58 |
| III | 0.226 | 54 | 0.316 | 7 | 2.20 | 2.23 | 2.27 | 2.31 | 2.36 |
| IV | 0.187 | 17 | 0.405 | 21 | 2.14 | 2.17 | 2.24 | 2.30 | 2.40 |
| V | 0.219 | 21 | 0.361 | 26 | 2.10 | 2.14 | 2.20 | 2.28 | 2.35 |
| VI | 0.266 | 22 | 0.324 | 16 | 2.11 | 2.17 | 2.23 | 2.32 | 2.45 |
| VII | 0.201 | 17 | 0.365 | 24 | 2.08 | 2.14 | 2.19 | 2.27 | 2.37 |
| VIII | 0.218 | 47 | 0.326 | 12 | 2.12 | 2.14 | 2.18 | 2.23 | 2.27 |
| IX | 0.135 | 51 | 0.209 | 10 | 1.83 | 1.86 | 1.89 | 1.92 | 1.95 |
| X | 0.230 | 39 | 0.298 | 24 | 2.03 | 2.07 | 2.11 | 2.17 | 2.21 |

for Region I (New England), the median estimate of σ_0^2 is 0.325, and the median estimate of ν_σ is 65. If these estimates are accurate, then (conditional on the model, of course) most counties in New England have about the same between-census-block variability—65 degrees of freedom is a fairly large number in the scaled inverse-chi-squared distribution. The lower estimate of ν_δ , 31, implies that some census blocks have more between-house variability than others do. The combination of the estimated variation in between-house variability and the estimated variation in between-block variability yields estimates of the variation in the GSDs within this region: as the table indicates, if the central parameter estimates are correct then in EPA’s Region I the median GSD is 2.71, and about 50% of GSDs fall between 2.61 and 2.82.

The uniformity of the GSD estimates across the entire U.S. is striking: almost all regions have median GSDs in the neighborhood of 2.2, and about half of the counties in the U.S. have GSDs between 2.15 and 2.35., with only regions I and IX deviating substantially from this pattern. Moreover, the partitioning of this variation into its components (within-block and between-block) is very similar across regions.

4.1 Uncertainties in the distributional parameters

Table 4 indicates only the central estimates of each parameter and the implied distribution of GSDs if these “best guess” values are actually true. But in fact, there is some uncertainty in some of the parameters— ν_σ and ν_δ in particular. If the true values are actually substantially lower than the central estimates, then the distributions of between-block and between-home-

within-block variances are wider, leading to more variability in county GSDs.

The most intuitive way to summarize the uncertainty in the distribution of GSDs is to consider how wide or narrow the distribution could be, given the uncertainties of the various parameters. For instance, in Region II we estimate that the 90th percentile of county GSDs is 2.58, but of course the true 90th percentile could instead be higher or lower than this value. What is the range in which we are fairly certain that the 90th percentile actually falls?

The uncertainties vary somewhat by region, but one standard error tends to be of the order of ± 0.08 for the 10th and 25th percentile GSD, ± 0.09 for the median, ± 0.10 for the 75th percentile, and ± 0.15 for the 90th percentile.

Actually the posterior distributions are not normal distributions, so that assuming normality doesn't quite give the right error bounds for a region containing 90% of the probability. For instance, the 10th percentile in Region II is almost certainly between 2.06 and 2.35 (the region containing the central 90% of probability), rather than between 2.02 and 2.37 as would obtain, given the standard error for the 10th percentile of 0.087 in this region, if the posterior distribution were normal.

As indicated above, although the estimates are reasonably certain for the 10th percentile and the median GSD in each region, there is much more uncertainty in just how high the highest GSDs in a region could be—the uncertainty in the 90th percentile is really fairly large. For instance, we cannot completely rule out the possibility that the most variable 10% of the counties in Region II could have GSDs over 2.8: the estimated 90th percentile in that region is 2.58, but with an uncertainty (one standard error) of ± 0.15 .

It is worth noting that GSDs of short-term “screening” data tend to be much higher than these estimates of true living-area-average GSDs, with observed county GSDs over 3.0 being fairly common for screening data. It has of course long been recognized that screening measurements are more variable than annual-average living-area measurements, due to temporal variability, lack of spatial averaging within the house, and so on. Still, we are aware of several cases (unpublished) in which state departments of health have used screening GSDs in conjunction with estimated county GMs in order to estimate the fraction of homes with living-area concentrations over a threshold such as 4 pCi/L. Since the screening GSDs tend to be much higher than the actual concentrations, this procedure will generally lead to a greatly elevated estimate of the fraction of homes exceeding the

reference level.

4.2 Model validation

Even before seeing the results, one might suspect several shortcomings in the statistical model. For example, it seems reasonable to think that counties that show unusually large variation between census block means (that is, counties with large values of σ_i) might also show unusually large variation between homes within census blocks (that is, high values of ϕ_{ij}).

The best way to include such a possibility would be to incorporate such a correlation in the model and explicitly estimate its magnitude. We have not done this. Instead, we fit the model without such a correlation, and examine the correlation between between- and within-block variability in the posterior distributions. This is not quite right, and will generally lead to an underestimate of the correlation, but at least we would expect to see gross effects if they were present. But in fact, there is no evidence of such an effect. To put it another way, any such effect then is small compared to the uncertainties in estimating it, since these uncertainties tend to be rather large. For a given county, some census blocks can be much more variable than others (the number of degrees of freedom ν_δ is below 20 in most regions), and since only 8 census blocks were monitored in each county if some blocks show more internal variability than others it is hard to tell whether the entire county shares this feature, or whether one or two blocks with unusually high variability simply happened to be sampled (or, for that matter, whether the extra variability is simply due to small-sample variation within the block). Thus the correlation between within- and between-block variability is swamped by the uncertainties in the various parameters.

A more serious problem is revealed by posterior predictive checks. In a posterior predictive check, the model is fit to the data, and then the parameters of the model are used to create simulated data. These simulated data are then compared to the actual data. The process seems circular—won't the simulated data match the actual data perfectly, since the simulated data are based on the fit to the actual data? The answer is “no”, because the model makes certain assumptions (normality, inverse-chi-squared distribution of variances, etc.), and if these assumptions are significantly violated then the simulated data will not agree with the observed data.

Unfortunately, this phenomenon actually occurs, notably for Regions I, II, and XI:

when we simulate data from the models, there are some noticeable differences between the simulated data and the actual observations. In particular, in these regions the highest observed GSDs within individual census blocks are consistently somewhat higher (of the order of 10% higher) than expected based on simulating from the model. Note that all of these regions have a large fraction of homes with very low radon measurements. Since the observed GSDs (and, via the model, the simulated GSDs) are sensitive to details of how such low measurements are handled, it seems likely that the poor model fit in these regions is due to inadequate modelling of the background subtraction effect. Unfortunately, this implies that the GSD parameter estimates in these regions are unreliable. In particular, we suspect that the true GSDs in Region I are considerably lower than the model implies, and those in Region IX may be substantially higher.

Model fit is much better in other regions, and we have much more confidence in the estimates for the rest of the country.

5 Conclusions

In most regions of the U.S., almost all county GSDs or annual-average living-area radon concentrations fall between 2.1 and 2.4. Possible exceptions include Region I (New England) and Region IX (the Southwest), but a more likely explanation for the deviation of the estimates in those regions is a lack of model fit for very low concentration measurements, due to background subtraction effects.

Both the within- and between-census-block variations are substantial. Even within a given census block, log-space variances tend to be about 0.3 to 0.4, implying coefficients of variation of $\exp(\sqrt{0.3}) = 1.7$ to $\exp(\sqrt{0.4}) = 1.9$. Thus, even if a census block GM is exactly known, there is a large amount of variation between individual homes in the census block. The number of degrees of freedom in the distribution describing the census block GSDs is small, suggesting that some census blocks are much more variable than others. This is not surprising, since all census blocks contain about the same number of people (of the order of 200) and thus vary greatly in spatial extent, and one expects that spatially large census blocks will be considerably more variable than spatially small ones, which may encompass only a single city block.

6 References

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A Relationship between GM/GSD and “exposure bins”.

Suppose counties are grouped into “exposure bins” based on geometric mean concentration. The individual homes in a given county will have radon concentrations that vary substantially about the GM, so although the county is in a particular bin the homes will be apportioned among all of the bins. Table 2 shows the fraction of homes in each of six bins, as a function of county GM, assuming a county GSD of 2.2. The bins used here are those used in Bogen (1992) in fitting a nonlinear dose-response model to lung cancer mortality data and radon measurements.

B Fraction of homes over 4 pCi/L, for various GMs and GSDs

The fraction of homes exceeding the EPA’s recommended action level of 4 pCi/L naturally varies as a function of GM and GSD (see table 3). Almost all county GSDs fall between 2.0 and 2.6, with most closer to the center of this range. The fraction of homes exceeding 4 pCi/L shows large relative variation (but small absolute variation) as a function of GSD when the GM is low; for higher values of GM, the relative variation is fairly small as a function of GSD—indeed, when the GM is exactly 4.0 pCi/L, the fraction of homes over 4 pCi/L is always 0.5, independent of the GSD. For practical purposes, the variation as a function of GSD is most important for GMs between 1.5 and 2.0: for counties with GMs under 1.5 pCi/L, under 10% of homes exceed 4 pCi/L so these counties would not likely be the focus of detailed study, whereas for homes over 2 pCi/L, over 20% of homes exceed 4 pCi/L so these counties are “at risk” no matter what the GSD. Only in the intermediate range can the GSD be the deciding factor in whether the county merits special attention based on the fraction of homes over 4 pCi/L.

Table 2: Fraction of homes in each exposure bin, as a function of county GM, assuming a county GSD of 2.2 and using the same bins as Bogen (1992). Horizontal lines separate GM regions in which different bins have a plurality of the homes. Note that for this GSD and these bins, the fifth bin never has a plurality. The GM increments by 0.2 for GM values above 2.4 pCi/L.

| GM pCi/L | < 0.394 pCi/L | 0.394–0.787 pCi/L | 0.787–1.38 pCi/L | 1.38–2.17 pCi/L | 2.17–3.15 pCi/L | > 3.15 pCi/L |
|-------------|------------------|----------------------|---------------------|--------------------|--------------------|-----------------|
| 0.1 | 0.959 | 0.037 | 0.004 | 0.000 | 0.000 | 0.000 |
| 0.2 | 0.805 | 0.154 | 0.034 | 0.006 | 0.001 | 0.000 |
| 0.3 | 0.635 | 0.254 | 0.084 | 0.020 | 0.005 | 0.001 |
| 0.4 | 0.492 | 0.312 | 0.137 | 0.042 | 0.012 | 0.004 |
| 0.5 | 0.381 | 0.336 | 0.184 | 0.068 | 0.022 | 0.010 |
| 0.6 | 0.297 | 0.338 | 0.220 | 0.094 | 0.034 | 0.018 |
| 0.7 | 0.233 | 0.326 | 0.246 | 0.119 | 0.047 | 0.028 |
| 0.8 | 0.185 | 0.307 | 0.264 | 0.142 | 0.062 | 0.041 |
| 0.9 | 0.147 | 0.285 | 0.274 | 0.162 | 0.076 | 0.056 |
| 1.0 | 0.119 | 0.262 | 0.278 | 0.179 | 0.090 | 0.073 |
| 1.1 | 0.096 | 0.239 | 0.278 | 0.192 | 0.103 | 0.091 |
| 1.2 | 0.079 | 0.217 | 0.274 | 0.203 | 0.116 | 0.110 |
| 1.3 | 0.065 | 0.197 | 0.268 | 0.212 | 0.127 | 0.131 |
| 1.4 | 0.054 | 0.179 | 0.260 | 0.218 | 0.137 | 0.152 |
| 1.5 | 0.045 | 0.162 | 0.251 | 0.222 | 0.146 | 0.173 |
| 1.6 | 0.038 | 0.146 | 0.242 | 0.225 | 0.154 | 0.195 |
| 1.7 | 0.032 | 0.132 | 0.231 | 0.226 | 0.161 | 0.217 |
| 1.8 | 0.027 | 0.120 | 0.221 | 0.226 | 0.167 | 0.239 |
| 1.9 | 0.023 | 0.109 | 0.211 | 0.224 | 0.172 | 0.261 |
| 2.0 | 0.020 | 0.099 | 0.201 | 0.222 | 0.177 | 0.282 |
| 2.1 | 0.017 | 0.090 | 0.191 | 0.219 | 0.180 | 0.304 |
| 2.2 | 0.015 | 0.082 | 0.181 | 0.216 | 0.182 | 0.324 |
| 2.3 | 0.013 | 0.074 | 0.172 | 0.212 | 0.184 | 0.345 |
| 2.4 | 0.011 | 0.068 | 0.163 | 0.208 | 0.186 | 0.365 |
| 2.6 | 0.008 | 0.056 | 0.146 | 0.198 | 0.187 | 0.404 |
| 2.8 | 0.006 | 0.047 | 0.131 | 0.188 | 0.186 | 0.441 |
| 3.0 | 0.005 | 0.040 | 0.118 | 0.178 | 0.184 | 0.475 |
| 3.2 | 0.004 | 0.034 | 0.105 | 0.168 | 0.181 | 0.508 |
| 3.4 | 0.003 | 0.029 | 0.095 | 0.158 | 0.177 | 0.539 |
| 3.6 | 0.003 | 0.024 | 0.085 | 0.148 | 0.172 | 0.567 |
| 3.8 | 0.002 | 0.021 | 0.077 | 0.139 | 0.167 | 0.594 |
| 4.0 | 0.002 | 0.018 | 0.069 | 0.130 | 0.162 | 0.619 |

Table 3: Fraction of homes exceeding 4 pCi/L, for various values of GM and GSD

| | | GSD | | | |
|----|-----|-------|-------|-------|-------|
| | | 2.0 | 2.2 | 2.4 | 2.6 |
| GM | 0.5 | 0.001 | 0.004 | 0.009 | 0.015 |
| | 1.0 | 0.023 | 0.039 | 0.057 | 0.073 |
| | 1.5 | 0.079 | 0.107 | 0.131 | 0.152 |
| | 2.0 | 0.159 | 0.190 | 0.214 | 0.234 |
| | 2.5 | 0.249 | 0.276 | 0.296 | 0.311 |
| | 3.0 | 0.339 | 0.358 | 0.371 | 0.382 |
| | 3.5 | 0.424 | 0.433 | 0.439 | 0.444 |

C Computer code for estimating the parameters

The following is computer code, in the “S” programming language, that was used to calculate the parameter estimates in this paper. Portions of the code will probably be understandable to anyone with programming experience, but some knowledge of S is needed to really make sense of it. One important note is that S is vector-oriented, so that for instance “phi” is an entire vector of values, and “ybar” is a vector of values; “ybar - phi” is a vector containing the componentwise difference between ybar and phi.

```
phil2.gibbs <- function(y,y.gr1,y.gr2,nu10,nu20,v10, v20, nrep) {  
  # gibbs sampler for means and variances that vary among groups  
  # nu10, v10: degrees of freedom and central estimate of variance  
  #           for census block effects (assumed inv-chisq distrib)  
  # nu20, v20: same as above, for within-block variances  
  # note: EACH subgroup defined by y.gr2 must have a unique entry in  
  # y.gr2...e.g., if y.gr1 <- c(1,1,1,1,2,2,2,2), then  
  # y.gr2 <- c(1,1,2,2,3,3,4,4), NOT y.gr2 <- c(1,1,2,2,1,1,2,2)  
  gr1list <- unique(y.gr1)  
  nthetas <- length(gr1list)  
  
  # within each group i, count number of subgroups  
  nphi <- rep(0,nthetas)  
  for (i in 1:nthetas) {  
    nphi[i] <- length(unique(y.gr2[y.gr1==gr1list[i]]))  
  }  
  nphis <- sum(nphi)  
  
  print(c(nthetas, nphis))  
  
  # calculate observed means, and initial variance estimates  
  theta <- rep(0,nthetas)  
  ybar <- rep(0,nphis)  
  v <- rep(1,nphis)
```

```

n <- rep(1,nphis)
gr2 <- rep(0,nphis)
whichct <- rep(0,nphis)
ij <- 0
for (i in 1:nthetas) {
  gr2list <- unique(y.gr2[y.gr1==gr1list[i]])
  asumi <- 0
  for(j in 1:nphi[i]) {
    ij <- ij+1
    okij <- y.gr1==gr1list[i] & y.gr2 == gr2list[j]
    n[ij] <- sum(okij)
    ybar[ij] <- mean(y[okij])
    v[ij] <- var(y[okij])
    whichct[ij] <- i
    gr2[ij] <- gr2list[j]
#    print(c(ij,n[ij],v[ij]))
    asumi <- asumi + ybar[ij]
    asumi <- asumi + ybar[ij]
  }
  theta[i] <- asumi/nphi[i]
}
v[is.na(v)] <- mean(v[!is.na(v)])
v[v<0.0001] <- mean(v)
print(c('mean, var of v[ij]',mean(v),var(v)))

igrp <- match(y.gr1,unique(y.gr1))
isubgrp <- match(y.gr2,gr2)
reorder <- match(gr2,sort(unique(y.gr2)))

print(igrp)
print(isubgrp)

```

```

print(c('ybar[1]',ybar[1]))
  sigma2 <- rep(v10,nthetas)
  phi <- rep(0,nphis)

mu <- mean(ybar)
tau <- var(ybar)

aout <- matrix(0,nrow=nrep,ncol=(2*nthetas+2*nphis+6))

for (jrep in 1:nrep) {
  # subgroup effects, given all other parameters, and
  # subgroup variances, given all other parameters

  aprec <- 1/sigma2[whichct] + n/v
  amean <- (n*(ybar-theta[whichct])/v)/aprec
  adf <- nu20 + n
  phi <- rnorm(n=nphis,mean=amean,sd=sqrt(1/aprec))
  #print(c(mean(phi),var(phi)))

  resid <- y - (theta[igrp]+phi[subgrp])
  vv <- unlist(tapply(resid^2,list(y.gr2),sum))

  #vv is in order by the value of y.gr2, which isn't what we want---
  #we need to retain the same order as y.gr2, so if y.gr2 is unsorted,
  #vv is unsorted in the same way. So put it back.
  vv <- vv[reorder]

  aterm <- (nu20*v20+vv)/(nu20+n)
  x <- rchisq(nphis,adf)
  v <- adf*aterm/x

```

```

# group effects, given all other parameters
# (given phi and v, each y is like an observation of theta)
scalres <- unlist(tapply(n*(ybar-phi)/v,list(whichct),sum))
precsum <- unlist(tapply(n/v,list(whichct),sum))
aprec <- 1/tau^2 + precsum
amean <- (mu/tau^2 + scalres)/aprec
theta <- rnorm(n=nthetas,mean=amean,sd=sqrt(1/aprec))
# now variance of subgroup effects within each group
# ( phi ~ N(0, sigma_i^2) )
adf <- nu10 + nphi
vv <- unlist(tapply(phi^2,list(whichct),sum))
aterm <- (nu10*v10 + vv)/(nu10 + nphi)
x <- rchisq(nthetas,adf)
sigma2 <- adf * aterm/x

# hyperparameters
# v10
# sigma2 ~ Inv-chisq(nu, s^2) --> s^2|sigma,nu is gamma-distributed
# (if noninformative prior):
beta <- nu10*sum(1/sigma2)/2
alpha <- nthetas*nu10/2 + 1
v10 <- rgamma(1,shape=alpha)/beta
#
# similarly for v20
beta <- nu20*sum(1/v)/2
alpha <- nphis*nu20/2 + 1
v20 <- rgamma(1,shape=alpha)/beta
#
# Now a metropolis step for the nu10 values:
nu10p <- exp(log(nu10) + rnorm(n=1,mean=0,sd=0.2))
corterm <- 0
# corterm <- log(nu10p) - log(nu10)

```

```

term1 <- nthetas*(nu10p*log(nu10p/2)-nu10*log(nu10/2))/2
term2 <- nthetas*(nu10p-nu10)*log(v10)/2
term3 <- (nu10-nu10p)*sum(log(sigma2))/2
term4 <- (nu10-nu10p)*v10*sum(1/sigma2)/2
term5 <- nthetas*log(gamma(nu10/2)/gamma(nu10p/2))
lgratio <- term1+term2+term3+term4+term5+corterm

if(lgratio > 0) {
  nu10 <- nu10p
  # print(round(c(term1,term2,term3,term4,term5,lgratio)))
} else {
  if (runif(n=1,min=0,max=1) < exp(lgratio)) {
    nu10 <- nu10p
  }
}

# metropolis step for nu20 values:
nu20p <- exp(log(nu20) + rnorm(n=1, mean=0, sd=0.2))
corterm <- 0
# corterm <- log(nu20p) - log(nu20)
term1 <- nphis*(nu20p*log(nu20p/2)-nu20*log(nu20/2))/2
term2 <- nphis*(nu20p-nu20)*log(v20)/2
term3 <- (nu20-nu20p)*sum(log(v))/2
term4 <- (nu20-nu20p)*v20*sum(1/v)/2
term5 <- nphis*log(gamma(nu20/2)/gamma(nu20p/2))
lgratio <- term1+term2+term3+term4+term5+ corterm

if(lgratio > 0) {
  nu20 <- nu20p
} else {
  if (runif(n=1,min=0,max=1) < exp(lgratio)) {
    nu20 <- nu20p
  }
}

```

```

    }
  }
  # now mu, tau
  mu <- rnorm(n=1, mean=mean(theta),sd=sqrt(tau/nthetas))
  tau2 <- sum((mu-theta)^2)/nthetas
  tau <- sqrt(nthetas*tau2 / rchisq(1,nthetas) )
  print(round(c(jrep,mu,tau^2,nu10,v10,nu20,v20),2))
  # note: we're returning tau (an s.d.), but also v10 and v20 (vars)
  aout[jrep,] <- c(theta,sigma2,phi,v,mu,tau,nu10,v10,nu20,v20)
} # end jrep loop
return(aout)
} # end function

```